

Volatility Index® Methodology: Cboe Volatility Index®

## Contents

Introduction	3
The VIX Index Attributes	3
Market Data	4
The VIX Index Calculation: Step-by-Step	5
<ul> <li>Step 2. Calculate the Interest Rates</li> <li>Step 3. Calculate the Near- and Next-Term Variances</li> </ul>	6 6
Sample Calculation for the VIX Index	6
Volatility Index Filtering Algorithm	11
Exception When VIX Index Cannot be Calculated	11
The Calculation of the Final Settlement Value for VIX Derivatives	11
Appendix 1: Complete SPX/SPXW Option Data Used in Sample VIX Index Calculation	13
Appendix 2: Individual Contributions — K0 = 1960	17
	Introduction  Volatility as a Tradable Asset: VIX Futures & Options  Supporting Documents  The VIX Index Attributes  Contracts Used for the Near and Next Terms and Their Selection Method  Market Data  Calculation and Dissemination  The VIX Index Calculation: Step-by-Step  Step 1. Select the Near- and Next-Term  Step 2. Calculate the Interest Rates  Step 3. Calculate the Near- and Next-Term Variances  Step 4. Calculate the VIX Index  Sample Calculation for the VIX Index  Volatility Index Filtering Algorithm  Exception When VIX Index Cannot be Calculated  The Calculation of the Final Settlement Value for VIX Derivatives  Appendix 1: Complete SPX/SPXW Option Data Used in Sample VIX Index Calculation  Appendix 2: Individual Contributions — K0 = 1960



## Introduction

In 1993, Cboe Global Markets, Incorporated® (Cboe®) introduced the Cboe Volatility Index® (VIX® Index). Originally designed to measure the market's expectation of 30-day volatility implied by at-the-money S&P 100® Index (OEX® Index) option prices, the VIX Index soon became the premier benchmark for U.S. stock market volatility. It is regularly featured in the Wall Street Journal, Barron's, and other leading financial publications, as well as business news shows on CNBC, Bloomberg TV, and CNN/Money, where the VIX Index is often referred to as the "fear gauge."

Ten years later in 2003, Cboe collaborated with Goldman Sachs to update the VIX Index. The changes reflected a new way to measure expected volatility, a methodology that continues to be widely used by financial theorists, risk managers, and volatility traders alike. The new VIX Index is based on the S&P 500® Index, the core index for U.S. equities, and estimates expected volatility by aggregating the weighted prices of S&P 500 Index puts and calls (SPX<sup>™</sup> options) over a wide range of strike prices. By supplying a script for replicating volatility exposure with a portfolio of SPX options, this new methodology transformed the VIX Index from an abstract concept into a practical standard for trading and hedging volatility.

## Volatility as a Tradable Asset: VIX Futures & Options

On March 24, 2004, Cboe introduced the first exchange-traded VIX futures contract on its new, all-electronic Cboe Futures Exchange (CFE®). Two years later in February 2006, VIX options were launched for trading on Cboe Options Exchange (C1).

The negative correlation of volatility to stock market returns is well-documented and suggests a diversification benefit to including volatility in an investment portfolio. VIX futures and options are designed to isolate expected volatility exposure in a single, efficient package. C1 and CFE provide continuous, liquid, and transparent markets for VIX products that are available to investors.

The rules and procedures applied to calculate the final settlement value of VIX derivatives vary slightly from that of the spot VIX Index calculation. For more information about those differences, refer to the section The Calculation of the Final Settlement Value for VIX Derivatives below.

## **Supporting Documents**

This Methodology references and should be read in conjunction with the following document:

**Cboe Volatility Index Mathematics Methodology** 

## The VIX Index Attributes

In this section, some of the configurations used for the Cboe Volatility Index® (VIX® Index) are provided.

## Contracts Used for the Near and Next Terms and Their Selection Method

The table below provides the attributes used for the near and next term selection for the VIX Index.

Index	Constant	Set of Contracts Used for Constituent Series Selection	Selection Method
	Maturity		
VIX	30 days	AM-settled SPX option contracts and PM-settled SPXW option contracts expiring at end of week, excluding the ones expiring on the same date as AM-settled SPX option contracts.	30 Day Bracket Method

#### Table Key

- Constant Maturity: reflects the target expected volatility term
- Set of Contracts Used for Constituent Series Selection: provides the initial set of series that are candidates for the near and next term selection

## Market Data

The table below provides the source of the market data for all options series used in the VIX Index calculation. The market data used can be sourced from a specific exchange, from a subset of exchanges or from among all available exchanges or trading venues reflecting the (National) Best Bid/Offer ((N)BBO) quotes.

Index	Market data source
VIX	Cboe Options Exchange (C1) only

## Calculation and Dissemination

The calculation and dissemination of volatility index values is determined by trading session, e.g., regular trading hours (RTH), global trading hours (GTH) or both. The trading session(s) and approximate dissemination and calculation time periods are listed below. These times may be modified due to shortened trading sessions, e.g., shortened holiday trading hours. Calculation and dissemination occur approximately four times per minute. A Business Day is defined as a day when the Cboe Options Exchange is open for the Cboe Regular Trading Hours (RTH) session. The Index follows the Cboe Options Exchange holiday schedule.

Index	Trading Session(s)	Approximate Calculation and Dissemination Time Period			
VIX	RTH	Between 9:31 a.m. and 4:15 p.m. ET			
	GTH	Between 3:15 a.m and 9:25 a.m. ET			

## The VIX Index Calculation: Step-by-Step

Stock indexes, such as the S&P 500 Index, are calculated using the prices of their component stocks. Each index employs rules that govern the selection of component securities and a formula to calculate index values.

The VIX Index is a volatility index comprised of options rather than stocks, with the price of each option reflecting the market's expectation of future volatility. Like conventional indexes, the VIX Index calculation employs rules for selecting component options and a formula to calculate index values.

The generalized formula used in the VIX Index calculation§ is:

$$\sigma^2 = \frac{2}{T} \sum_i \frac{\Delta K_i}{K_i^2} e^{RT} Q(K_i) - \frac{1}{T} \left[ \frac{F}{K_0} - 1 \right]^2$$

where

Ki=Ko.

σ	$VIX\ index = \sigma \times 100$	$\Delta K_i$	Interval between strike prices – half the difference between the strike on either side of $K_i$ :
T	Time to expiration (in years)		$K_{i+1} - K_{i-1}$
$\boldsymbol{F}$	Option-implied forward price		$\Delta K_i = \frac{K_{i+1} - K_{i-1}}{2}$
$K_{\circ}$	First strike equal to or otherwise immediately below the		
	ward index level, F	R	Risk-free interest rate to expiration
101	ward mackievely.		
$K_i$	Strike price of the <i>i</i> <sup>th</sup> out-of-the-money option; a call if K <sub>i</sub> > K <sub>0</sub> and a put if K <sub>i</sub> < K <sub>0</sub> ; both put and call if	$Q(K_i)$	The midpoint of the bid-ask spread for each option with strike Ki.



<sup>§</sup> Please see "More than you ever wanted to know about volatility swaps" by Kresimir Demeterfi, Emanuel Derman, Michael Kamal, and Joseph Zou, Goldman Sachs Quantitative Strategies Research Notes, March 1999.

The VIX Index measures 30-day expected volatility of the S&P 500 Index. The calculation takes as input the market prices of SPX options and SPXW options as well as U.S. Treasury yield curve rates. The VIX Index value can be obtained by following the four steps below:

## Step 1. Select the Near- and Next-Term

The inputs required for this step are provided in the above section, "Contracts Used and Exclusion Criteria for the Near and Next Terms." The universe of options that can be selected as components of the VIX Index are all AM-settled SPX option contracts and PM-settled SPXW option contracts expiring at end of week, excluding the ones expiring on the same date as AM-settled SPX option contracts. Using a constant maturity term of 30 days, apply the rules for selecting the correct near- and next-terms found in section 1(a) Bracket Method of the Cboe Volatility Index Mathematics Methodology document.

## Step 2. Calculate the Interest Rates

The risk-free interest rates, R1 and R2, are based on U.S. Treasury yield curve rates (commonly referred to as "Constant Maturity Treasury" rates, or CMTs), to which a cubic spline is applied to derive yields on the expiration dates of relevant SPX options. As such, the VIX Index calculation may use different risk-free interest rates for near- and next-term options. The rules for calculating the interest rates for the near- and next-terms can be found in section 2(a) Interest Rate Calculation – Bounded Cubic Spline Interpolation of the Cboe Volatility Index Mathematics Methodology.

## Step 3. Calculate the Near- and Next-Term Variances

The inputs for calculating the variances ( $\sigma^2$ ) for both terms are based on the options series defined in Step 1 above. These include the corresponding bid, ask, and options price for each options series, where options price is defined as the midpoint of the bid / ask quotes, and the corresponding interest rates defined in Step 2 above. Given these inputs, the variances for the near- and next-terms can be calculated by following the steps outlined in section 3(a) Volatility Index Calculation – Single Term of the Cboe Volatility Index Mathematics Methodology.

## Step 4. Calculate the VIX Index

The inputs for calculating the VIX Index are based on the near- and next-term expiration dates defined in Step 1 above, the variances for each term calculated in Step 3 above, and the constant maturity term of 30 days. Given these inputs, the VIX Index can be calculated by following the steps outlined in section 3(b) Volatility Index Calculation – Constant Maturity Term of the Cboe Volatility Index Mathematics Methodology.

## Sample Calculation for the VIX Index

In this section, we implement a sample calculation for the VIX Index using the process outlined above.

#### • Select the Near- and Next-Term Constituent Series

In this hypothetical example, assume that the calculation is performed on trade date of September 27<sup>th</sup>, 2022 at 10:45:15 a.m. ET. Given the inputs described in the Step 1 above, and the methodology in section 1(a) of the Cboe Volatility Index Mathematics Methodology, the selected terms for this calculation are the "standard" SPX options expiring on October 21<sup>st</sup>, 2022 for the near term and the P.M.-settled SPX Weeklys expiring on the following week (October 28, 2022) for the next term. In this example, the near-term SPX constituent series expire in 24 calendar days and the next-term SPXW constituent series expire in 31 calendar days.

#### • Calculate the Interest Rates

Assume that the yield curve rates provided below are available on September 26<sup>th</sup>, 2022 at the end of the day.

Date	1 Mo	2 Mo	3 Mo	6 Mo	1 Yr	2 Yr	3 Yr	5 Yr	7 Yr	10 Yr	20 Yr	30 Yr
9/26/2022	0.03	0.02	0.04	0.05	0.08	0.11	0.22	0.59	1.00	1.37	2.03	2.21

Given these yield curve rates, and the rules outlined in the section 2(a) of the Cboe Volatility Index Mathematics Methodology, the results are  $R_1 = 0.031664\%$  for the near-term options and  $R_2 = 0.028797\%$  for the next-term options.

#### Calculate the Single Term Variances

Time to Expiration

Note that "standard" SPX options are deemed to expire at the open of trading (i.e., 9:30 a.m. ET) on their expiration date (the third Friday of the month or the day before if Holiday). "Weekly" SPXW options are deemed to expire at the close of trading (i.e., 4:00 p.m. ET) on their expiration dates (typically every Friday except third Fridays of the month or the day before if Holiday).

Following the steps in Time to Expiration of section 3(a)(i) Volatility Index Calculation – Single Term in the Cboe Volatility Index Mathematics Methodology and applying 10:45:15 a.m. ET as the time of the calculation, the time to expiration for the near-term and next-term options,  $T_1$  and  $T_2$ , respectively, are:

$$T_1 = 34,484 / 525,600 = 0.0656088$$

$$T_2 = 44,954 / 525,600 = 0.0855289$$

Forward Price and K<sub>0</sub>

Using the call and put prices for the near-term and next-term options below and following the steps in Forward Price and  $K_0$  in section 3(a)(ii) Volatility Index Calculation – Single Term of the Cboe Volatility Index Mathematics Methodology, we can calculate the forward price and  $K_0$ .

Near-Term Options						
Strike Price	Call	Put	Difference			
1940	38.45	15.25	23.20			
1945	34.70	16.55	18.15			
1950	31.10	18.25	12.85			
1955	27.60	19.75	7.85			
1960	24.25	21.30	2.95			
1965	21.05	23.15	2.10			
1970	18.10	25.05	6.95			
1975	15.25	27.30	12.05			
1980	12.75	29.75	17.00			

Next-Term Options					
Strike Price	Call	Put	Difference		
1940	41.05	18.80	22.25		
1945	37.45	20.20	17.25		
1950	34.05	21.60	12.45		
1955	30.60	23.20	7.40		
1960	27.30	24.90	2.40		
1965	24.15	26.90	2.75		
1970	21.10	28.95	7.85		
1975	18.30	31.05	12.75		
1980	15.70	33.50	17.80		

The ATM strike for the near-term options is **1965** and the ATM strike for the next-term options is **1960**. Applying their respective call and put prices to the formula

$$F =$$
Strike Price +  $e^{RT} \times$  (Call Price – Put Price)

gives that the forward index prices,  $F_1$  and  $F_2$ , for the near- and next-term options, respectively, are:

$$F_1 = 1965 + e^{(0.000317 \times 0.0656088)} \times (21.05 - 23.15) = 1962.89996$$

$$F_2 = 1960 + e^{(0.000288 \times 0.0855289)} \times (27.30 - 24.90) = 1962.40006$$

We have then that  $K_0$ , the strike price equal to or immediately below the forward index level F, is **1960** for the near-term options and **1960** for the next-term options.

#### Strike Selection

To determine the strikes to be included in this calculation, refer to the steps in Strike Selection of section 3(a)(iii) Volatility Index Calculation – Single Term in the Cooe Volatility Index Mathematics Methodology.

First, for each term, select out-of-the-money put options with strike prices less than  $K_0$ . Start with the put strike immediately lower than  $K_0$  and move to successively lower strike prices. Exclude any put option that has a bid price equal to zero (i.e., no bid). As shown below, once two puts with consecutive strike prices are found to have zero bid prices, exclude the observed put(s) and consider no puts with lower strikes for inclusion. (Note that the 1350 and 1355 put options are not included despite having non-zero bid prices.)

Put Strike	Bid	Ask	Include?	
1345	0	0.15		
1350	0.05	0.15	Not considered following two zero bids	
1355	0.05	0.35	bius	
1360	0	0.35	No	
1365	0	0.35	No	
1370	0.05	0.35	Yes	
1375	0.1	0.15	Yes	
1380	0.1	0.2	Yes	

Next, select out-of-the-money call options with strike prices greater than  $K_0$ . Start with the call strike immediately higher than  $K_0$  and move to successively higher strike prices, excluding call options that have a bid price of zero (i.e., no bid). As with the puts, once two call options with consecutive strike prices are found to have zero bid prices, exclude the observed call(s) and consider no calls with higher strikes for inclusion. (Note that the 2225 call option is not included despite having a non-zero bid price.)

Call Strike	Bid	Ask	Include?	
2095	0.05	0.35	Yes	
2100	0.05	0.15	Yes	
2120	0	0.15	No	
2125	0.05	0.15	Yes	
2150	0	0.1	No	
2175	0	0.05	No	
2200	0	0.05		
2225	0.05	0.1	Not considered following two zero bids	
2250	0	0.05		

Finally, select **both** the put and call with strike price  $K_0$ . Notice that two options are selected at  $K_0$ , while a single option, either a put or a call, is used for every other strike price.

The following tables contain the options used to calculate the VIX Index in this example. This calculation uses the midpoint of quoted bid and ask prices for each option selected. The  $K_0$  put and call prices are averaged to produce a single value. The price used for the 1960 strike in the near-term is, therefore, (24.25 + 21.30) / 2 = 22.775. The price used for the 1960 strike in the next term is (27.30 + 24.90) / 2 = 26.10.

Near-Term Strike	Option Type	Midpoint Price
1370	Put	0.2
1375	Put	0.125
1380	Put	0.15
1950	Put	18.25
1955	Put	19.75
1960	Put/Call Average	22.775
<b>1960</b> 1965	Put/Call Average Call	<b>22.775</b> 21.05
1965	Call	21.05
1965 1970	Call Call	21.05
1965 1970	Call Call	21.05 18.1

Next-Term Strike	Option Type	Midpoint Price
1275	Put	0.075
1325	Put	0.15
1350	Put	0.15
1950	Put	21.60
1955	Put	23.20
1960	Put/Call Average	26.10
1965	Call	24.15
1970	Call	21.10
2125	Call	0.1
2150	Call	0.1
2200	Call	0.08

### Calculating Volatility

The VIX Index is an amalgam of the information reflected in the prices of all of the selected options. The contribution of a single option to the VIX Index value is proportional to  $\Delta K$  and the price of that option, and inversely proportional to the square of the option's strike price.

Referring to Calculating Volatility of section 3(a)(iv) Volatility Index Calculation – Single Term of the Cboe Volatility Index Mathematics Methodology, we generally have that  $\Delta K_i$  is half the difference between the strike prices on either side of  $K_i$ . For example, the  $\Delta K$  for the next-term 1325 Put is 37.5:  $\Delta K_{1325 \, \mathrm{Put}} = (1350 - 1275) / 2$ . At the upper and lower edges of any given strip of options,  $\Delta K_i$  is simply the difference between  $K_i$  and the adjacent strike price. In this example, the 1370 Put is the lowest strike in the strip of near-term options and 1375 is the adjacent strike. Therefore,  $\Delta K_{1370 \, \mathrm{Put}} = 5$  (i.e., 1375 – 1370).

The contribution of the near-term 1370 Put is given by:

$$\frac{\Delta K_{1370 Put}}{K_{1370 Put}^2} e^{R_1 T_1} Q(1370 Put)$$

$$\frac{\Delta K_{1370 Put}}{K_{1370 Put}^2} e^{R_1 T_1} Q(1370 Put) = \frac{5}{(1370)^2} e^{0.000317 (0.0656088)} (0.2) = 0.0000005328$$

A similar calculation is performed for each option. The resulting values for the near-term options are then summed and multiplied by  $2/T_1$ . Likewise, the resulting values for the next-term options are summed and multiplied by  $2/T_2$ . The tables below summarize the results for each set of options.

Near-Term Strike	Option Type	Midpoint Price	Contribution by Strike
1370	Put	0.2	0.0000005328
1375	Put	0.125	0.0000003306
1380	Put	0.15	0.0000003938
1950	Put	18.25	0.0000239979
1955	Put	19.75	0.0000258376
1960	Put/Call Average	22.775	0.0000296432
1965	Call	21.05	0.0000272588
1970	Call	18.1	0.0000233198
2095	Call	0.2	0.0000002278
2100	Call	0.1	0.0000003401
2125	Call	0.1	0.0000005536
$\frac{2}{T_1}$	0.019267		

Next-Term Strike	Option Type	Midpoint Price	Contribution by Strike
1275	Put	0.075	0.0000023069
1325	Put	0.15	0.0000032041
1350	Put	0.15	0.0000020577
1950	Put	21.6	0.0000284031
1955	Put	23.2	0.0000303512
1960	Put/Call Average	26.1	0.0000339711
1965	Call	24.15	0.0000312732
1970	Call	21.1	0.0000271851
2125	Call	0.1	0.000005536
2150	Call	0.1	0.0000008113
2200	Call	0.075	0.0000007748
$\frac{2}{T_2}$	0.019441		

Next calculate  $^1\!/_T\!\left[^F\!/_{K_0}-1\right]^2$  for the near-term (T1) and next-term (T2):

$$\frac{1}{T_1} \left[ \frac{F_1}{K_{0,1}} - 1 \right]^2 = \frac{1}{0.0656088} \left[ \frac{1962.89996}{1960} - 1 \right]^2 = 0.00003337$$

$$\frac{1}{T_2} \left[ \frac{F_2}{K_{0,2}} - 1 \right]^2 = \frac{1}{0.0855289} \left[ \frac{1962.40006}{1960} - 1 \right]^2 = 0.00001753$$

Now calculate  $\sigma^2$ 1 and  $\sigma^2$ 2:

$$\sigma_1^2 = \frac{2}{T_1} \sum_i \frac{\Delta K_i}{K_i^2} e^{R_1 T_1} Q(K_i) - \frac{1}{T_1} \left[ \frac{F_1}{K_{0,1}} - 1 \right]^2 = 0.019267 - 0.00003337 = 0.019233906$$

$$\sigma_2^2 = \frac{2}{T_2} \sum_i \frac{\Delta K_i}{K_i^2} e^{R_2 T_2} Q(K_i) - \frac{1}{T_2} \left[ \frac{F_2}{K_{0,2}} - 1 \right]^2 = 0.019441 - 0.00001753 = 0.019423884$$

#### Calculate the VIX Index

The VIX Index value is now calculated by following section 3(b) Volatility Index Calculation – Constant Maturity Term of the Cboe Volatility Index Mathematics Methodology. First, calculate the 30-day weighted average of  $\sigma^2$  and  $\sigma^2$ . Then take the square root of that value and multiply by 100:

$$\textit{VIX} = 100 \times \sqrt{\left\{0.0656088 \times 0.019233906 \times \left[\frac{44,954 - 43,200}{44,954 - 34,484}\right] + 0.0855289 \times 0.019423884 \times \left[\frac{43,200 - 34,484}{44,954 - 34,484}\right]\right\} \times \frac{525,600}{43,200}} \times \left[\frac{100,0000}{100,0000} \times \left[\frac{100,0000}{100,0$$

$$VIX = 100 \times 0.13927842 = 13.93$$



## Volatility Index Filtering Algorithm

As described above, "spot" VIX Index values are based on the average of SPX/SPXW option bid / ask quotes ("mid-quote" prices), and only options that have a non-zero bid price are included. The bid-ask spread is generally accepted as a current indication of market price, and the average of the bid and ask quotes can be thought of as an indication of "fair" value. Spot VIX Index values are calculated using mid-quote options prices.

From time to time, options price quotations widen due to changing market conditions, technology failures, or other reasons. When this occurs, options that were previously included in a VIX Index value calculation might be excluded due to them now having a zero bid price. In other instances, the mid-quote prices of one or more SPX/SPXW options might materially change. This can result in a VIX Index value that, while accurately reflecting SPX/SPXW options quotes at the time, may not reflect the expected volatility of the S&P 500 Index. Cboe uses a filtering algorithm to address these circumstances.

For the rules that guide this filtering process, refer to the details given in section "Index Level Filtering Algorithm" of the Cboe Volatility Index Mathematics Methodology. At a minimum annually, we review the thresholds used in the Index Level Filtering Algorithm to consider their reflection of market conditions, and may, in our discretion, change these thresholds as a result, by notice to clients from time to time. The inputs itemized below apply to the VIX Index:

Index	Session	Threshold Level (x)	Threshold Period
VIX	RTH	0.50 volatility points	2 minutes
VIX	GTH	0.50 volatility points	5 minutes

## Exception When VIX Index Cannot be Calculated

In the event the VIX Index cannot be calculated, the last calculated and disseminated spot VIX Index value is republished until a new valid spot VIX Index can be calculated. The conditions that would prevent the VIX Index from being calculated can be found in sections 3(a) (ii) and (iii) Volatility Index Calculation – Single Term of the Cboe Volatility Index Mathematics Methodology. A summary can also be found in the section 4(b) Volatility Index Cannot be Calculated of the Cboe Volatility Index Mathematics Methodology.

## The Calculation of the Final Settlement Value for VIX Derivatives

The final settlement value for VIX futures and options is determined on the morning of their expiration date (usually a Wednesday) through a Special Opening Quotation ("SOQ") of the VIX Index. There are several ways in which the calculation of the SOQ of the VIX Index differs from the calculation of the spot VIX Index at all other times.

- The SOQ calculation uses SPX, or SPXW, options from a single expiration 30 calendar days for the subject settlement day. Unlike the spot VIX Index calculation at other times, the SOQ calculation does not involve theinterpolation of volatility calculated with near-term and next-term options.
- Unlike the spot VIX Index calculation at other times, the determination of the strike range used for the SOQ calculation does not depend on whether options with consecutive strikes have zero bid prices. Cboe determines and announces the highest call strike and the lowest put strike that establish the "strike range" to be used in the SOQ calculation. It does so by using an algorithm to determine the call with the highest strike and the put with the lowest strike to be used in that calculation. The strike prices used in the SOQ calculation include all put options within the strike range that have a strike price less than  $K_0$ , all call options within the strike range that have a strike price greater than  $K_0$ , and both the put and call options that have a strike price equal to  $K_0$ . Importantly, options within the Cboe-determined strike range with a zero bid price are eligible to be included in the SOQ calculation, which also differs from the calculation of the spot VIX Index at other times.



• The SOQ calculation uses the "opening trade price" of each of the selected options, as determined pursuant to Cboe's rules during the special opening auction that Cboe conducts on days when VIX derivatives settle. This approach is different from the mid-quote prices that are used to calculate the spot VIX Index at all other times. Cboe uses the mid-quote price in the SOQ calculation only if a selected option does not have an opening price, in which case Cboe uses the midpoint price of the highest bid and lowest offer at the time of the opening. When calculating the forward index price, the mid-quote price is based on the best-bid and best-offer (BBO).

For more information about VIX Derivatives settlement, visit http://www.cboe.com/products/vix-index-volatility/vix-options-and-futures/vix-index/vix-faqs.

# Appendix 1: Complete SPX/SPXW Option Data Used in Sample VIX Index Calculation Option series included in the VIX Index calculation are highlighted.

	No	ear-Term Optio	ns	
	Calls		Pu	its
Strike	Bid	Ask	Bid	Ask
800	1160.90	1164.40	0.00	0.10
900	1060.90	1064.50	0.00	0.10
1000	961.00	964.50	0.00	0.10
1050	911.00	914.50	0.00	0.10
1100	861.00	864.60	0.00	0.05
1125	836.00	839.60	0.00	0.05
1150	811.00	814.60	0.00	0.05
1175	786.10	789.60	0.00	0.05
1200	761.10	764.60	0.00	0.05
1220	741.10	744.60	0.00	0.10
1225	736.10	739.60	0.00	0.05
1240	721.10	724.60	0.00	0.10
1250	711.10	714.60	0.00	0.05
1260	701.10	704.60	0.00	0.10
1270	691.10	694.60	0.00	0.10
1275	686.10	689.60	0.00	0.10
1280	681.10	684.60	0.00	0.10
1290	671.10	674.70	0.00	0.10
1300	661.10	664.70	0.05	0.10
1305	656.10	659.70	0.00	0.10
1310	651.10	654.70	0.00	0.10
1315	646.10	649.70	0.00	0.10
1320	641.20	644.70	0.00	0.10
1325	636.20	639.70	0.05	0.10
1330	631.20	634.70	0.00	0.10
1335	626.20	629.70	0.00	0.15
1340	621.20	624.70	0.00	0.15
1345	616.20	619.70	0.00	0.15
1350	611.20	614.70	0.05	0.15
1355	606.20	609.70	0.05	0.35
1360	601.20	604.70	0.00	0.35
1365	596.20	599.70	0.00	0.35
1370	591.20	594.70	0.05	0.35
1375	586.20	589.70	0.10	0.15
1380	581.20	584.70	0.10	0.20
1385	576.20	579.70	0.10	0.35
1390	571.20	574.70	0.10	0.35
1395	566.20	569.70	0.10	0.15
1400	561.20	564.80	0.10	0.15
1405	556.20	559.80	0.00	0.35
1410	551.20	554.80	0.05	0.40
1415	546.20	549.80	0.00	0.40
1420	541.20	544.80	0.05	0.40
1425	536.30	539.80	0.15	0.20

Next-Term Options						
Cautha	Calls			Puts		
Strike	Bid	Ask	Bid	Ask		
1225	735.90	738.80	0.00	0.10		
1250	710.80	713.80	0.00	0.10		
1275	686.00	688.70	0.05	0.10		
1300	660.90	663.80	0.00	0.10		
1325	635.90	638.60	0.10	0.20		
1350	610.90	613.60	0.10	0.20		
1375	585.90	588.70	0.10	0.25		
1400	561.00	563.70	0.15	0.25		
1425	536.00	538.80	0.20	0.30		
1450	511.10	513.80	0.25	0.35		
1475	486.10	488.90	0.30	0.40		
1500	461.20	464.00	0.35	0.45		
1510	451.30	454.00	0.35	0.50		
1520	441.30	444.00	0.40	0.50		
1525	436.30	439.10	0.40	0.55		
1530	431.30	434.10	0.45	0.55		
1540	421.40	424.10	0.45	0.60		
1550	411.40 406.40	414.20	0.50	0.60		
1555	406.40	409.20	0.50	0.65		
1560			0.55	0.65		
1565 1570	396.50 391.20	399.20 394.00	0.55	0.70		
1575	386.50	389.30	0.60	0.75		
1580	381.50	384.30	0.60	0.75		
1585	376.60	379.30	0.65	0.75		
1590	371.30	374.10	0.65	0.80		
1595	366.60	369.40	0.70	0.80		
1600	361.60	364.40	0.70	0.85		
1605	356.70	359.40	0.75	0.85		
1610	351.70	354.50	0.75	0.90		
1615	346.70	349.50	0.80	0.90		
1620	341.80	344.50	0.80	0.95		
1625	336.80	339.50	0.85	0.95		
1630	331.80	334.60	0.90	1.00		



Near-Term Options (cont.)				
		ılls		ıts
Strike	Bid	Ask	Bid	Ask
1430	531.30	534.80	0.05	0.40
1435	526.30	529.80	0.15	0.40
1440	521.30	524.80	0.05	0.30
1445	516.30	519.80	0.05	0.40
1450	511.30	514.80	0.15	0.25
1455	506.30	509.80	0.05	0.45
1460	501.30	504.80	0.05	0.45
1465	496.30	499.80	0.05	0.45
1470	491.30	494.80	0.05	0.45
1475	486.30	489.90	0.15	0.25
1480	481.30	484.90	0.05	0.45
1485	476.30	479.90	0.20	0.50
1490	471.30	474.90	0.05	0.30
1495	466.40	469.90	0.05	0.50
1500	461.40	464.90	0.25	0.40
1505	456.40	459.90	0.30	0.35
1510	451.40	454.90	0.05	0.55
1515	446.40	449.90	0.05	0.55
1520	441.40	445.00	0.10	0.60
1525	436.40	440.00	0.30	0.40
1530	431.40	435.00	0.05	0.60
1535	426.40	430.00	0.10	0.65
1540	421.40	425.00	0.10	0.65
1545	416.50	420.00	0.10	0.65
1550	411.50	415.00	0.30	0.70
1555	406.50	410.10	0.15	0.70
1560	401.50	405.10	0.15	0.70
1565	396.50	400.10	0.15	0.70
1570	391.50	395.10	0.20	0.75
1575	386.50	390.10	0.35	0.75
1580	381.50	385.10	0.25	0.80
1585	376.60	380.20	0.25	0.80
1590	371.60	375.20	0.25	0.80
1595	366.60	370.20	0.25	0.80
1600	361.60	365.20	0.50	0.85
1605	356.60	360.30	0.30	0.85
1610	351.60	355.30	0.35	0.90
1615	346.70	350.30	0.35	0.90
1620	341.70	345.30	0.35	0.90
1625	336.70	340.40	0.40	0.95
1630	331.70	335.40	0.40	0.95
1635	326.70	330.40	0.45	1.00
1640	321.80	325.40	0.45	1.00
1645	316.80	320.50	0.50	1.05
1650	311.80	315.50	0.50	0.85
1655	306.80	310.50	0.55	1.10
1660	301.90	305.60	0.55	1.10
1665	296.90	300.60	0.60	1.15

	Next-	Term Options (	(cont.)	
a	Ca	alls	Pt	ıts
Strike	Bid	Ask	Bid	Ask
1635	326.90	329.60	0.90	1.05
1640	321.90	324.70	0.95	1.05
1645	316.90	319.70	0.95	1.10
1650	312.00	314.70	1.00	1.15
1655	307.00	309.80	1.05	1.15
1660	302.10	304.80	1.10	1.20
1665	297.10	299.90	1.15	1.25
1670	292.20	294.90	1.15	1.30
1675	287.20	289.90	1.20	1.35
1680	282.30	285.00	1.25	1.40
1685	277.30	280.10	1.30	1.45
1690	272.40	275.10	1.35	1.50
1695	267.40	270.20	1.40	1.55
1700	262.50	265.20	1.45	1.60
1705	257.50	260.30	1.50	1.70
1710	252.60	255.30	1.60	1.75
1715	247.70	250.40	1.65	1.80
1720	242.70	245.50	1.70	1.90
1725	237.80	240.60	1.75	1.95
1730	232.90	235.60	1.85	2.00
1735	228.00	230.70	1.90	2.10
1740	223.40	225.30	2.00	2.20
1745	218.50	220.40	2.10	2.25
1750	213.60	215.50	2.20	2.35
1755	208.70	210.60	2.30	2.45
1760	203.80	205.70	2.40	2.55
1765	198.90	200.80	2.50	2.65
1770	194.00	195.90	2.65	2.80
1775	189.20	191.10	2.75	2.90
1780	184.30	185.80	2.90	3.10
1785	179.40	180.90	3.00	3.20
1790	174.60	176.10	3.10	3.40
1795	169.70	171.20	3.30	3.60
1800	164.90	166.40	3.50	3.70
1805	160.10	161.60	3.70	3.90
1810	155.30	156.70	3.80	4.10
1815	150.50	152.00	4.10	4.30
1820	145.70	147.20	4.30	4.50
1825	140.90	142.40	4.50	4.80
1830	136.20	137.70	4.80	5.00
1835	131.50	132.90	5.00	5.30
1840	126.80	128.20	5.30	5.60
1845	122.10	123.50	5.60	5.90
1850	117.40	118.80	5.90	6.20
1855	112.80	114.20	6.30	6.60
1860	108.20	109.60	6.60	6.90
1865	103.60	105.00	7.00	7.30
1870	99.00	100.40	7.50	7.80



Near-Term Options (cont.)				
A	Ca	Ils	Pu	ıts
Strike	Bid	Ask	Bid	Ask
1670	291.90	295.70	0.60	1.15
1675	287.00	290.70	0.65	1.20
1680	282.00	285.70	0.70	1.25
1685	277.00	280.80	0.75	1.30
1690	272.10	275.80	0.75	1.30
1695	267.10	270.90	0.80	1.35
1700	262.10	265.90	0.85	1.40
1705	257.20	261.00	0.85	1.40
1710	252.20	256.00	0.90	1.45
1715	247.30	251.10	0.95	1.50
1720	242.30	246.10	1.00	1.55
1725	237.40	241.20	1.05	1.60
1730	232.40	236.30	1.10	1.65
1735	227.50	231.30	1.15	1.70
1740	222.50	226.40	1.20	1.75
1745	217.60	221.50	1.25	1.85
1750	212.60	216.60	1.30	1.90
1755	207.70	211.60	1.40	1.95
1760	202.80	206.70	1.45	2.05
1765	197.80	201.80	1.50	2.15
1770	192.90	196.90	1.60	2.20
1775	188.00	192.00	1.65	2.35
1780	183.10	187.10	1.75	2.40
1785	178.20	182.20	1.85	2.50
1790	173.30	177.30	1.90	2.60
1795	168.40	172.40	2.00	2.75
1800	163.50	167.50	2.15	2.90
1805	158.60	162.60	2.25	3.00
1810	153.80	157.80	2.35	3.20
1815	148.90	152.90	2.50	3.40
1820	144.10	148.10	2.65	3.50
1825	139.20	143.30	3.00	3.60
1830	134.40	138.40	3.00	3.90
1835	129.60	133.60	3.20	4.10
1840	124.80	128.80	3.40	4.40
1845	120.10	124.10	3.60	4.60
1850	115.40	119.30	3.80	4.90
1855	110.60	114.60	4.10	5.20
1860	105.90	109.90	4.40	5.50
1865	101.30	105.20	4.70	5.80
1870	96.60	100.50	5.00	6.20
1875	92.00	95.90	5.40	6.60
1880	87.40	91.30	5.80	7.00
1885	82.90	86.70	6.20	7.50
1890	78.40	82.20	6.70	8.00
1895	74.00	77.70	7.20	8.60
1900	69.60	73.20	7.80	8.80
1905	66.00	68.50	8.50	9.50

	Next-Term Options (cont.)				
		ills		ıts	
Strike	Bid	Ask	Bid	Ask	
1875	94.50	95.90	8.00	8.30	
1880	90.00	91.40	8.40	8.80	
1885	85.50	86.90	9.00	9.40	
1890	81.10	82.50	9.50	10.00	
1895	76.80	78.10	10.20	10.60	
1900	72.40	73.70	10.90	11.30	
1905	68.20	69.40	11.60	12.00	
1910	64.00	65.20	12.40	12.80	
1915	59.80	61.10	13.20	13.70	
1920	55.70	57.00	14.20	14.60	
1925	51.70	53.00	15.20	15.60	
1930	47.80	49.10	16.20	16.60	
1935	44.60	45.10	17.40	17.80	
1940	40.80	41.30	18.60	19.00	
1945	37.20	37.70	20.00	20.40	
1950	33.70	34.40	21.40	21.80	
1955	30.30	30.90	23.00	23.40	
1960	27.00	27.60	24.70	25.10	
1965	23.80	24.50	26.50	27.30	
1970	20.80	21.40	28.50	29.40	
1975	18.00	18.60	30.50	31.60	
1980	15.50	15.90	33.00	34.00	
1985	13.10	13.50	35.50	36.60	
1990	10.90	11.30	38.40	39.50	
1995	9.00	9.30	41.30	42.50	
2000	7.20	7.60	44.50	45.80	
2005	5.70	6.00	48.10	49.30	
2010	4.50	4.80	51.70	53.00	
2015	3.40	3.70	55.80	57.00	
2020	2.60	2.80	59.90	61.70	
2025	1.95	2.15	64.10	66.10	
2030	1.45	1.65	68.60	70.60	
2035	1.05	1.25	73.30	75.20	
2040	0.80	0.95	78.00	80.00	
2045	0.60	0.75	82.00	84.80	
2050	0.50	0.65	86.90	89.60	
2060	0.30	0.40	96.60	99.40	
2070	0.20	0.30	106.70	109.50	
2075	0.15	0.25	111.70	114.50	
2100	0.10	0.20	136.30	139.10	
2125	0.05	0.15	161.50	164.30	
2150	0.05	0.15	186.30	189.00	
2175	0.00	0.10	211.30	214.00	
2200	0.05	0.10	236.30	239.00	
2225	0.00	0.10	261.30	264.00	
2250	0.00	0.10	286.30	289.00	



	Near-	Term Options (	cont.)	
		ills	Pu	ıts
Strike	Bid	Ask	Bid	Ask
1910	61.60	64.10	9.10	10.20
1915	57.40	59.80	9.90	11.30
1920	53.30	55.60	10.70	12.10
1925	49.10	51.20	11.60	12.60
1930	45.20	47.30	12.50	14.00
1935	41.20	43.40	13.60	14.70
1940	37.40	39.50	14.70	15.80
1945	33.70	35.70	15.90	17.20
1950	30.10	32.10	17.70	18.80
1955	26.70	28.50	19.00	20.50
1960	23.40	25.10	20.60	22.00
1965 1970	20.30	21.80	22.30	24.00
1970	17.40	18.80 15.90	24.30	25.80
1980	12.20	13.30	28.90	30.60
1985	9.90		31.40	
1990		11.00		33.20 36.50
1990	7.90 6.20	9.00 7.10	34.30 37.40	39.70
			40.70	
2000	4.70	5.20		43.20
2005	3.40	4.20	44.00	47.70
2010	2.65	3.10	48.00	51.40
2015	1.75	2.30	52.20	56.00
2020	1.20	1.70	56.60	60.40
2025	1.00	1.25	61.20	65.00
2030	0.45	0.80	65.90	69.70 74.40
2035	0.25		70.70	
2040	0.35	0.65	75.60 80.50	79.30 84.10
2043	0.20	0.30	85.40	
2055	0.20	0.50	90.40	89.00 94.00
		0.30		98.90
2060	0.15	0.30	95.30	103.90
2070	0.10	0.20	105.30	103.90
2075	0.10	0.20	110.30	113.80
2073	0.05	0.20	115.30	118.80
2085	0.05	0.40	120.30	123.80
2090	0.05	0.40	125.30	128.80
2095	0.05	0.35	130.30	133.80
2100	0.05	0.15	135.30	138.80
2120	0.00	0.15	155.30	158.80
2125	0.05	0.15	160.30	163.80
2150	0.00	0.10	185.20	188.80
2175	0.00	0.10	210.20	213.70
2200	0.00	0.05	235.20	238.70
2225	0.05	0.10	260.20	263.70
2250	0.00	0.05	285.20	288.70



# Appendix 2: Individual Contributions — $K_0$ = 1960

Near-				
Term	Option Type	Midpoint	Delta-K	Contribution
Strike		Price		by Strike
1370	Put	0.2	5	0.0000005328
1375	Put	0.125	5	0.0000003306
1380	Put	0.15	5	0.0000003938
1385	Put	0.225	5	0.0000005865
1390	Put	0.225	5	0.0000005823
1395	Put	0.125	5	0.0000003212
1400	Put	0.125	7.5	0.0000004783
1410	Put	0.225	10	0.0000011318
1420	Put	0.225	7.5	0.0000008369
1425	Put	0.175	5	0.0000004309
1430	Put	0.225	5	0.000005502
1435	Put	0.275	5	0.0000006677
1440	Put	0.175	5	0.0000004220
1445	Put	0.225	5	0.0000005388
1450	Put	0.2	5	0.0000004756
1455	Put	0.25	5	0.0000005905
1460	Put	0.25	5	0.0000005864
1465	Put	0.25	5	0.0000005824
1470	Put	0.25	5	0.0000005785
1475	Put	0.2	5	0.0000004596
1480	Put	0.25	5	0.0000005707
1485	Put	0.35	5	0.0000007936
1490	Put	0.175	5	0.0000003941
1495	Put	0.275	5	0.0000006152
1500	Put	0.325	5	0.0000007222
1505	Put	0.325	5	0.0000007174
1510	Put	0.3	5	0.0000006579
1515	Put	0.3	5	0.0000006535
1520	Put	0.35	5	0.0000007575
1525	Put	0.35	5	0.0000007525
1530	Put	0.325	5	0.0000006942
1535	Put	0.375	5	0.0000007958
1540	Put	0.375	5	0.0000007938
1545	Put	0.375	5	0.0000007908
1550	Put	0.575	5	0.0000007833
1555	Put	0.3	5	0.0000010408
1560	Put	0.425	5	0.0000008788
1565			5	
1505	Put	0.425		0.0000008676
	Put	0.475	5	0.0000009635
1575	Put	0.55	5	0.0000011086
1580	Put	0.525	5	0.0000010515
1585	Put	0.525	5	0.0000010449
1590	Put	0.525	5	0.0000010384
1595	Put	0.525	5	0.0000010319
1600	Put	0.675	5	0.0000013184
1605	Put	0.575	5	0.0000011161
1610	Put	0.625	5	0.0000012056
1615	Put	0.625	5	0.0000011982

Next-				
Term	Option Type	Midpoint Price	Delta-K	Contribution by Strike
Strike		Price		ру Зипке
1275	Put	0.075	50	0.0000023069
1325	Put	0.15	37.5	0.0000032041
1350	Put	0.15	25	0.0000020577
1375	Put	0.175	25	0.0000023141
1400	Put	0.2	25	0.0000025511
1425	Put	0.25	25	0.0000030779
1450	Put	0.3	25	0.0000035673
1475	Put	0.35	25	0.0000040219
1500	Put	0.4	17.5	0.0000031112
1510	Put	0.425	10	0.000018640
1520	Put	0.45	7.5	0.0000014608
1525	Put	0.475	5	0.0000010213
1530	Put	0.5	7.5	0.0000016020
1540	Put	0.525	10	0.0000022137
1550	Put	0.55	7.5	0.0000017170
1555	Put	0.575	5	0.0000011890
1560	Put	0.6	5	0.0000012328
1565	Put	0.625	5	0.0000012759
1570	Put	0.65	5	0.0000013185
1575	Put	0.675	5	0.0000013606
1580	Put	0.675	5	0.0000013520
1585	Put	0.7	5	0.0000013932
1590	Put	0.725	5	0.0000014339
1595	Put	0.75	5	0.0000014741
1600	Put	0.775	5	0.0000015137
1605	Put	0.8	5	0.0000015528
1610	Put	0.825	5	0.0000015914
1615	Put	0.85	5	0.0000016295
1620	Put	0.875	5	0.0000016671
1625	Put	0.9	5	0.0000017042
1630	Put	0.95	5	0.0000017878
1635	Put	0.975	5	0.0000018237
1640	Put	1	5	0.0000018591
1645	Put	1.025	5	0.0000018940
1650	Put	1.075	5	0.0000019743
1655	Put	1.1	5	0.0000020081
1660	Put	1.15	5	0.0000020867
1665	Put	1.2	5	0.0000021644
1670	Put	1.225	5	0.0000021963
1675	Put	1.275	5	0.0000022723
1680	Put	1.325	5	0.0000023474
1685	Put	1.375	5	0.0000024215
1690	Put	1.425	5	0.0000024947
1695	Put	1.475	5	0.0000025670
1700	Put	1.525	5	0.0000026385
1705	Put	1.6	5	0.0000027520
1710	Put	1.675	5	0.0000028642
1715	Put	1.725	5	0.0000029325
L	1	1	l .	1

Near-Term Strike         Option Type         Midpoint Price         Delta-K         Contributory Strike           1620         Put         0.625         5         0.000001           1625         Put         0.675         5         0.000001           1630         Put         0.675         5         0.000001           1635         Put         0.725         5         0.000001           1640         Put         0.725         5         0.000001           1645         Put         0.775         5         0.000001           1650         Put         0.825         5         0.000001           1660         Put         0.825         5         0.000001           1660         Put         0.875         5         0.000001           1670         Put         0.875         5         0.000001           1675         Put         0.925         5         0.000001           1680         Put         1.025         5         0.000001           1690         Put         1.025         5         0.000001	ike 11908 12781 12703 13561 13478 14320 12397 15060
1625         Put         0.675         5         0.000001           1630         Put         0.675         5         0.000001           1635         Put         0.725         5         0.000001           1640         Put         0.725         5         0.000001           1645         Put         0.775         5         0.000001           1650         Put         0.675         5         0.000001           1655         Put         0.825         5         0.000001           1660         Put         0.825         5         0.000001           1665         Put         0.875         5         0.000001           1670         Put         0.925         5         0.000001           1680         Put         0.975         5         0.000001           1685         Put         1.025         5         0.000001	12781 12703 13561 13478 14320 12397 15060
1630         Put         0.675         5         0.000001           1635         Put         0.725         5         0.000001           1640         Put         0.725         5         0.000001           1645         Put         0.775         5         0.000001           1650         Put         0.675         5         0.000001           1655         Put         0.825         5         0.000001           1660         Put         0.825         5         0.000001           1665         Put         0.875         5         0.000001           1670         Put         0.875         5         0.000001           1675         Put         0.925         5         0.000001           1680         Put         0.975         5         0.000001           1685         Put         1.025         5         0.000001	12703 13561 13478 14320 12397 15060
1635         Put         0.725         5         0.000001           1640         Put         0.725         5         0.000001           1645         Put         0.775         5         0.000001           1650         Put         0.675         5         0.000001           1655         Put         0.825         5         0.000001           1660         Put         0.825         5         0.000001           1665         Put         0.875         5         0.000001           1670         Put         0.875         5         0.000001           1680         Put         0.925         5         0.000001           1685         Put         1.025         5         0.000001	13561 13478 14320 12397 15060
1640         Put         0.725         5         0.000001           1645         Put         0.775         5         0.000001           1650         Put         0.675         5         0.000001           1655         Put         0.825         5         0.000001           1660         Put         0.825         5         0.000001           1665         Put         0.875         5         0.000001           1670         Put         0.875         5         0.000001           1675         Put         0.925         5         0.000001           1680         Put         0.975         5         0.000001           1685         Put         1.025         5         0.000001	13478 14320 12397 15060
1645         Put         0.775         5         0.000001           1650         Put         0.675         5         0.000001           1655         Put         0.825         5         0.000001           1660         Put         0.825         5         0.000001           1665         Put         0.875         5         0.000001           1670         Put         0.875         5         0.000001           1675         Put         0.925         5         0.000001           1680         Put         0.975         5         0.000001           1685         Put         1.025         5         0.000001	14320 12397 15060 14970
1650         Put         0.675         5         0.000001           1655         Put         0.825         5         0.000001           1660         Put         0.825         5         0.000001           1665         Put         0.875         5         0.000001           1670         Put         0.875         5         0.000001           1675         Put         0.925         5         0.000001           1680         Put         0.975         5         0.000001           1685         Put         1.025         5         0.000001	12397 15060 14970
1655         Put         0.825         5         0.000001           1660         Put         0.825         5         0.000001           1665         Put         0.875         5         0.000001           1670         Put         0.875         5         0.000001           1675         Put         0.925         5         0.000001           1680         Put         0.975         5         0.000001           1685         Put         1.025         5         0.000001	15060 14970
1660         Put         0.825         5         0.000001           1665         Put         0.875         5         0.000001           1670         Put         0.875         5         0.000001           1675         Put         0.925         5         0.000001           1680         Put         0.975         5         0.000001           1685         Put         1.025         5         0.000001	14970
1665         Put         0.875         5         0.000001           1670         Put         0.875         5         0.000001           1675         Put         0.925         5         0.000001           1680         Put         0.975         5         0.000001           1685         Put         1.025         5         0.000001	
1670         Put         0.875         5         0.000001           1675         Put         0.925         5         0.000001           1680         Put         0.975         5         0.000001           1685         Put         1.025         5         0.000001	.5782
1675         Put         0.925         5         0.000001           1680         Put         0.975         5         0.000001           1685         Put         1.025         5         0.000001	
1680         Put         0.975         5         0.000001           1685         Put         1.025         5         0.000001	5688
1685 Put 1.025 5 0.000001	6485
	7273
1690 Put 1.025 5 0.000004	8051
1030 rut 1.025 5 0.000001	7944
1695 Put 1.075 5 0.000001	8709
1700 Put 1.125 5 0.000001	19464
1705 Put 1.125 5 0.000001	19350
<b>1710</b> Put 1.175 5 0.000002	20092
<b>1715</b> Put 1.225 5 0.000002	20825
<b>1720</b> Put 1.275 5 0.000002	21549
<b>1725</b> Put 1.325 5 0.000002	22265
<b>1730</b> Put 1.375 5 0.000002	22972
<b>1735</b> Put 1.425 5 0.000002	23670
<b>1740</b> Put 1.475 5 0.000002	24360
<b>1745</b> Put 1.55 5 0.000002	25452
<b>1750</b> Put 1.6 5 0.000002	26123
<b>1755</b> Put 1.675 5 0.000002	27192
<b>1760</b> Put 1.75 5 0.000002	28248
<b>1765</b> Put 1.825 5 0.000002	29292
<b>1770</b> Put 1.9 5 0.000003	80324
1775 Put 2 5 0.000003	31740
<b>1780</b> Put 2.075 5 0.000003	32746
1785 Put 2.175 5 0.000003	34132
<b>1790</b> Put 2.25 5 0.000003	35112
<b>1795</b> Put 2.375 5 0.000003	86856
1800 Put 2.525 5 0.000003	88967
1805 Put 2.625 5 0.000004	10286
<b>1810</b> Put 2.775 5 0.000004	12353
1815 Put 2.95 5 0.000004	14776
<b>1820</b> Put 3.075 5 0.000004	16417
<b>1825</b> Put 3.3 5 0.000004	19541
1830 Put 3.45 5 0.000005	
1835 Put 3.65 5 0.000005	
1840 Put 3.9 5 0.000005	
1845 Put 4.1 5 0.000006	

Individual Contributions (Cont.)				
Next- Term Strike	Option Type	Midpoint Price	Delta-K	Contribution by Strike
1720	Put	1.8	5	0.0000030423
1725	Put	1.85	5	0.0000031087
1730	Put	1.925	5	0.0000032160
1735	Put	2	5	0.0000033221
1740	Put	2.1	5	0.0000034682
1745	Put	2.175	5	0.0000035715
1750	Put	2.275	5	0.0000037144
1755	Put	2.375	5	0.0000038556
1760	Put	2.475	5	0.0000039951
1765	Put	2.575	5	0.0000041330
1770	Put	2.725	5	0.0000043491
1775	Put	2.825	5	0.0000044833
1780	Put	3	5	0.0000047344
1785	Put	3.1	5	0.0000048648
1790	Put	3.25	5	0.0000050718
1795	Put	3.45	5	0.0000053539
1800	Put	3.6	5	0.0000055557
1805	Put	3.8	5	0.0000058319
1810	Put	3.95	5	0.0000060287
1815	Put	4.2	5	0.0000063749
1820	Put	4.4	5	0.0000066419
1825	Put	4.65	5	0.0000069808
1830	Put	4.9	5	0.0000073160
1835	Put	5.15	5	0.0000076474
1840	Put	5.45	5	0.0000080490
1845	Put	5.75	5	0.0000084461
1850	Put	6.05	5	0.0000088388
1855	Put	6.45	5	0.0000093724
1860	Put	6.75	5	0.0000097557
1865	Put	7.15	5	0.0000102785
1870	Put	7.65	5	0.0000109385
1875	Put	8.15	5	0.0000115914
1880	Put	8.6	5	0.0000121664
1885	Put	9.2	5	0.0000129463
1890	Put	9.75	5	0.0000136478
1895	Put	10.4	5	0.0000144809
1900	Put	11.1	5	0.0000153743
1905	Put	11.8	5	0.0000162582
1910	Put	12.6	5	0.0000172697
1915	Put	13.45	5	0.0000183386
1920	Put	14.4	5	0.0000195317
1925	Put	15.4	5	0.0000207797
1930	Put	16.4	5	0.0000220146
1935	Put	17.6	5	0.0000235034
1940	Put	18.8	5	0.0000249767
1945	Put	20.2	5	0.0000266989

Individual Contributions (Cont.)				
Near- Term	Option Type	Midpoint Price	Delta-K	Contribution by Strike
Strike 1850	Put	4.35	5	0.0000063551
1855	Put	4.65	5	0.0000063531
1860	Put	4.95	5	0.0000071542
1865	Put	5.25	5	0.0000075471
1870	Put	5.6	5	0.0000080073
1875	Put	6	5	0.0000085335
1880	Put	6.4	5	0.0000090541
1885	Put	6.85	5	0.0000096393
1890	Put	7.35	5	0.0000102883
1895	Put	7.9	5	0.0000109999
1900	Put	8.3	5	0.0000114961
1905	Put	9	5	0.0000124003
1910	Put	9.65	5	0.0000132263
1915	Put	10.6	5	0.0000144526
1920	Put	11.4	5	0.0000154626
1925	Put	12.1	5	0.0000163269
1930	Put	13.25	5	0.0000177861
1935	Put	14.15	5	0.0000188962
1940	Put	15.25	5	0.0000202603
1945	Put	16.55	5	0.0000218745
1950	Put	18.25	5	0.0000239979
1955	Put	19.75	5	0.0000258376
1960	Put/Call Average	22.775	5	0.0000296432
1965	Call	21.05	5	0.0000272588
1970	Call	18.1	5	0.0000233198
1975	Call	15.25	5	0.0000195486
1980	Call	12.75	5	0.0000162614
1985	Call	10.45	5	0.0000132609
1990	Call	8.45	5	0.0000106691
1995	Call	6.65	5	0.0000083544
2000	Call	4.95	5	0.0000061876
2005	Call	3.8	5	0.0000047264
2010	Call	2.875	5	0.0000035582
2015	Call	2.025	5	0.0000024938
2020	Call	1.45	5	0.0000017768
2025	Call	1.125	5	0.0000013718
2030	Call	0.725	5	0.0000008797
2035	Call	0.525	5	0.0000006339
2040	Call	0.5	5	0.0000006007
2045	Call	0.4	5	0.0000004782
2050	Call	0.25	5	0.0000002974
2055	Call	0.325	5	0.0000003848
2060	Call	0.225	5	0.0000002651
2065	Call	0.175	5	0.0000002052
2070	Call	0.15	5	0.000001750
2075	Call	0.15	5	0.000001742

Individual Contributions (Cont.)				
Next- Term Strike	Option Type	Midpoint Price	Delta-K	Contribution by Strike
1950	Put	21.6	5	0.0000284031
1955	Put	23.2	5	0.0000303512
1960	Put/Call Average	26.1	5	0.0000339711
1965	Call	24.15	5	0.0000312732
1970	Call	21.1	5	0.0000271851
1975	Call	18.3	5	0.0000234584
1980	Call	15.7	5	0.0000200240
1985	Call	13.3	5	0.0000168776
1990	Call	11.1	5	0.0000140151
1995	Call	9.15	5	0.0000114952
2000	Call	7.4	5	0.0000092502
2005	Call	5.85	5	0.0000072763
2010	Call	4.65	5	0.0000057549
2015	Call	3.55	5	0.0000043718
2020	Call	2.7	5	0.0000033086
2025	Call	2.05	5	0.0000024997
2030	Call	1.55	5	0.0000018807
2035	Call	1.15	5	0.0000013885
2040	Call	0.875	5	0.0000010513
2045	Call	0.675	5	0.0000008070
2050	Call	0.575	7.5	0.0000010262
2060	Call	0.35	10	0.0000008248
2070	Call	0.25	7.5	0.0000004376
2075	Call	0.2	15	0.0000006968
2100	Call	0.15	25	0.0000008504
2125	Call	0.1	25	0.0000005536
2150	Call	0.1	37.5	0.0000008113
2200	Call	0.075	50	0.0000007748

	Individual Contributions (Cont.)			
Near- Term Strike	Option Type	Midpoint Price	Delta-K	Contribution by Strike
2080	Call	0.25	5	0.0000002889
2085	Call	0.225	5	0.0000002588
2090	Call	0.1	5	0.0000001145
2095	Call	0.2	5	0.0000002278
2100	Call	0.1	15	0.0000003401
2125	Call	0.1	25	0.0000005536

Sum of Individual Contributions for near term: 0.0006320516

$$\frac{2}{T_1} \sum_{i} \frac{\Delta K_i}{K_i^2} e^{R_1 T_1} Q(K_i) = 0.019267$$

Sum of Individual Contributions for next term: 0.0008314016 
$$\frac{2}{T_2} \sum_i \frac{\Delta K_i}{K_i^2} \ e^{R_2 T_2} Q(K_i) = 0.019441$$

#### **Disclosures and Disclaimers Related to Choe Indices**

Cboe Global Indices, LLC and Cboe Europe Indices, B.V. (collectively, the "Cboe Index Providers", and individually a "Cboe Index Provider"), are both subsidiaries of Cboe Global Markets, Inc. (Cboe Global Markets, Inc., the Cboe Index Providers, and the other subsidiaries and affiliates of Cboe Global Markets, Inc. are collectively referred to herein as the "Cboe Companies" and those entities are individually referred to as a "Cboe Company").

The Cboe Index Providers are each an index provider that administers, calculates and distributes indices and other values (as applicable) (collectively, "Cboe Indices" and individually a "Cboe Index"). Additional information regarding the Cboe Index Providers and their operations is available at <a href="https://www.cboe.com/indices/">www.cboe.com/indices/</a>.

Nothing herein constitutes an offer of services. The information herein is provided solely for informational purposes. Choe Indices are calculated and administered (as described in relevant methodologies, rules and other information) without regard to the needs of any particular person, entity, or group of persons, using market information, including, without limitation, market data from exchanges owned and operated by other Cboe Companies.

Index and benchmark values for dates or time periods prior to an index launch date, if any, are calculated using a theoretical approach involving back-testing historical data in accordance with the methodology in place on the launch date (unless otherwise stated). Back-testing involves the theoretical application of the index methodology in hindsight and therefore does not involve actual performance and may not produce performance commensurate with prospective application of the methodology. No back-tested approach can completely account for the impact of decisions that might have been made if calculations were made at the same time as certain underlying market conditions occurred. Supporting documentation for statements, comparisons, statistics or other technical data provided in this document is available by request at <a href="https://www.cboe.com/contact/">www.cboe.com/contact/</a>.

Past performance of an index or financial product is not indicative of future results. Indices are not financial products that can be invested in directly, but they can be used as the basis for financial products (for example, without limitation, options, futures, mutual funds or exchange-traded funds) or to help manage portfolios.

The Cboe Index Providers are not investment advisers or tax advisers. No decision to buy, hold, or sell any financial product should be made in reliance on any of the information provided herein, and no representation is made regarding the advisability or tax consequences of any investment, whether based on an index or not. Nothing herein should be construed as investment advice. No representation or assurance is made that any financial product will accurately track the performance of an underlying index or provide positive investment returns. Index values and returns are theoretical, and do not reflect the results of actual trading of financial products, nor the value of an actual portfolio, and may not reflect the fees, taxes or other expenses associated with buying, holding or selling investments or the effect of actual market conditions or events. The Cboe Index Providers are not broker-dealers, intermediaries, investment firms or securities exchanges and they do not manage actual financial products. None of the Cboe Companies sponsor, endorse, promote, manage, sell or administer any financial product that is created, sponsored, issued or sold by a third-party, whether based on any Cboe Index or not.

No data, values, or other content contained herein ("Content") may be copied, modified, reverse-engineered, reproduced, distributed, or stored in a database or retrieval system, in any form or by any means, nor may any Content be used to create a derivative work (e.g., a financial product, service or index) or used to verify or correct other data or information, without the Cboe Index Provider's prior written consent. Without derogating from the aforementioned, Content shall not be used for any unlawful or unauthorized purposes.

The Cboe Companies, their third-party service or data providers, or any party from whom they have licensed trademarks or indices (collectively, the "Cboe Parties") do not guarantee the accuracy, completeness, or timeliness of the Content, trademarks, strategies or values, or the methodologies or input data used to calculate index values. The Cboe Parties are not responsible for any errors or omissions, regardless of the cause, or for the results obtained from the use of the Content, index strategies or values, methodologies or input data. THE CONTENT, INDICES AND RELATED STRATEGIES AND METHODOLOGIES ARE PROVIDED "AS IS" WITHOUT WARRANTY OF ANY KIND, EITHER EXPRESS OR IMPLIED, INCLUDING, WITHOUT LIMITATION, ANY WARRANTY WITH RESPECT TO MERCHANTABILITY OR FITNESS FOR A PARTICULAR PURPOSE OR USE. USERS OF CONTENT AND/OR THE CBOE INDICES BEAR ALL RISKS OF LOSS.

WITHOUT LIMITING THE FOREGOING AND TO THE MAXIMUM EXTENT PERMITTED BY APPLICABLE LAW, IN NO EVENT SHALL THE CBOE PARTIES BE RESPONSIBLE OR LIABLE TO ANY PERSON OR ENTITY FOR ANY DAMAGES OF ANY KIND, INCLUDING, BUT NOT LIMITED TO, DIRECT, INDIRECT, SPECIAL, INCIDENTAL, CONSEQUENTIAL, PUNITIVE, LOST PROFITS OR LOST OPPORTUNITIES, WHETHER OR NOT A CBOE PARTY HAS BEEN ADVISED OF THE POSSIBILITY OF SUCH DAMAGES. THE FOREGOING LIMITATIONS SHALL APPLY REGARDLESS OF WHETHER A CLAIM ARISES IN CONTRACT, TORT, NEGLIGENCE, STRICT LIABILITY, OR OTHERWISE.

The Cboe Index Providers receive compensation in connection with licensing Cboe Indices to third parties and providing calculation services to third parties. Some Cboe Companies operate markets for the trading of financial products and provide services to many organizations, including issuers of securities, investment advisers, broker-dealers, investment banks, other financial institutions and financial intermediaries, and accordingly may provide or receive fees or other economic benefits to or from those organizations. These organizations may also be Cboe Index Provider licensees or customers, and the Cboe Index Providers may include securities of or relating to such organizations in Cboe Indices.

Cboe®, C2<sup>SM</sup>, Cboe Clear<sup>SM</sup>, Cboe Closing Cross®, Cboe Digital<sup>SM</sup>, Cboe LIS®, Cboe Futures Exchange<sup>SM</sup>, Cboe Global Indices<sup>SM</sup>, Cboe Global Markets®, Cboe Options Institute®, Cboe Volatility Index®, Bats®, BIDS Trading®, Buffer Protect<sup>SM</sup>, BuyWrite<sup>SM</sup>, BYX®, BZX®, CFE®, EDGA®, EDGX®, Eris Exchange®, ErisX®, f(t)options<sup>SM</sup>, FLEX®, FLexible EXchange®, Hanweck<sup>SM</sup>, Hybrid®, LiveVol®, NANO®, Options Institute®, PutWrite<sup>SM</sup>, Silexx®, SRVIX<sup>SM</sup>, Trade Alert<sup>SM</sup>,

VIX®, and XSPSM are trademarks and service marks of the Cboe Companies. Trademarks of the Cboe Companies may only be used with written permission, subject to applicable Cboe Company trademark usage guidelines as published from time to time. Third-party trademarks and service marks used in this document are described below. The values and methodologies for indices branded with the "Cboe" trademark are the property of the relevant Cboe Index Provider.

The Cboe Companies have licensed several trademarks from third parties from whom they have also licensed indices which may be included in this document or in other materials related to Cboe Indices, as follows:

- Dow Jones®, Dow Jones Industrial Average® and DJIA® are trademarks or service marks of Dow Jones Trademark Holdings LLC ("<u>Dow Jones</u>"), have been licensed for use for certain purposes by the Cboe Companies. Derivative indices created, used and distributed by Cboe Companies and any investment products based thereon are not sponsored, endorsed, sold or promoted by Dow Jones, and Dow Jones makes no representation regarding the advisability of investing in any investment product that is based on any such derivative indices.
- FTSE® and the FTSE indices are trademarks and service marks of FTSE International Limited, used under license.
- IHS, IHS Markit, CDX, iBoxx, and iTraxx are trademarks of IHS Markit Limited and its affiliates ("IHS") and have been licensed for use by the Cboe Companies. Any IHS Markit index referenced herein is the property of IHS Markit and is used under license. Any products that have an IHS Markit index as their underlying interest are not sponsored, endorsed, or promoted by IHS Markit.
- MSCI and the MSCI index names are service marks of MSCI Inc. ("MSCI") or its affiliates and have been licensed for use by the Cboe Companies. Any derivative indexes and any financial products based on the derivative indexes ("Products") are not sponsored, guaranteed or endorsed by MSCI, its affiliates or any other party involved in, or related to, making or compiling such MSCI index. Neither MSCI, its affiliates nor any other party involved in, or related to, making or compiling any MSCI index makes any representations regarding the advisability of investing in such Products; or any warranty, express or implied; or bears any liability as to the results to be obtained by any person or any entity from the use of any such MSCI index or any data included therein. No purchaser, seller or holder of any Product, or any other person or entity, should use or refer to any MSCI trade name, trademark or service mark to sponsor, endorse, market or promote Products without first contacting MSCI to determine whether MSCI's permission is required.
- Nasdaq®, Nasdaq-100®, and Nasdaq-100 Index®, are trademarks of Nasdaq, Inc. (together with its affiliates, the "Corporations") and are licensed for use by Cboe Exchange, Inc. The CBOE Nasdaq-100 Volatility Index (the "Volatility Index") and CBOE Nasdaq-100 BuyWrite Index (the "BuyWrite Index") are not derived, maintained, published, calculated or disseminated by the Corporations. Neither the Volatility Index, the BuyWrite Index nor any product based on such indexes have been passed on by the Corporations as to their legality or suitability. Such products are not issued, endorsed, sold, or promoted by the Corporations. THE CORPORATIONS MAKE NO WARRANTIES AND BEAR NO LIABILITY WITH RESPECT TO THE VOLATILITY INDEX OR BUYWRITE INDEX.
- Russell, Russell 1000®, Russell 2000®, Russell 3000® and Russell MidCap® are registered trademarks of the Frank Russell Company, used under license.
- S&P, S&P 500, US500, 500, THE 500, SPDR, SPX, and DSPX are trade names or trademarks of S&P Dow Jones Indices, LLC or its affiliates ("<u>S&P</u>"). Any products that have an S&P index as their underlying interest are not sponsored, endorsed, sold or promoted by S&P and S&P makes no representation regarding the advisability of investing in any investment product that is based on any such indices.

© 2024 Choe Exchange, Inc. and its affiliates. All Rights Reserved.

v20230405

