Cboe


## Volatility Index ${ }^{\circledR}$ Methodology: Cboe 1-Day Volatility Index ${ }^{\circledR}$

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## Introduction

In 1993, Cboe Global Markets, Incorporated ${ }^{\circledR}$ (Cboe ${ }^{\circledR}$ ) introduced the Cboe Volatility Index ${ }^{\circledR}$ (VIX ${ }^{\circledR}$ Index). Originally designed to measure the market's expectation of 30-day volatility implied by at-the-money S\&P $100^{\circledR}$ Index (OEX ${ }^{\circledR}$ Index) option prices, the VIX Index soon became the premier benchmark for U.S. stock market volatility. It is regularly featured in the Wall Street Journal, Barron's, and other leading financial publications, as well as business news shows on CNBC, Bloomberg TV, and CNN/Money, where the VIX Index is often referred to as the "fear gauge."

Ten years later in 2003, Cboe collaborated with Goldman Sachs to update the VIX Index. The changes reflected a new way to measure expected volatility, a methodology that continues to be widely used by financial theorists, risk managers, and volatility traders alike. The new VIX Index is based on the S\&P $500^{\circledR}$ Index, the core index for U.S. equities, and estimates expected volatility by aggregating the weighted prices of S\&P 500 Index puts and calls (SPX ${ }^{\text {TM }}$ options) over a wide range of strike prices. By supplying a script for replicating volatility exposure with a portfolio of SPX options, this new methodology transformed the VIX Index from an abstract concept into a practical standard for trading and hedging volatility.

Similar to the VIX Index, the Cboe 1-Day Volatility Index ${ }^{\circledR}$ (VIX1D Index) estimates expected volatility by aggregating the weighted prices of P.M.-settled S\&P 500 Index $\left(S^{\prime} X^{S M}\right)$ puts and calls over a wide range of strike prices. The prices used to calculate VIX1D Index values are midpoints of real-time, P.M.-settled SPX (SPXW) option bid/ask price quotations. Because the period of expected volatility being measured is a single day, the P.M.-settled SPX option series that are used during the majority of the day that the VIX1D Index is calculated and disseminated include those where the expiry date is equal to the current day of the calculation (near-term expiration) and those with an expiry date closest to and after the near-term expiration (next term expiration). For example, during a business week with no holiday closures, the VIX1D Index calculated on a Tuesday, would use that Tuesday's expiration as the near-term option and that Wednesday's expiration (next term) expiration occurring during that week as the next-term option.

The VIX1D Index has been designed to account for the compressed measurement of expected volatility over a single day and differs from the VIX Index in ways to account for this. These differences include:

## Time Decay of Near-Term (Current Day Expiry) Options Used to Calculate the VIX1D Index

Through a given day, the time to expiration of the near-term (current day expiry) declines to zero when these option contracts expire, typically at 4:00 p.m. ET, which impacts the calculation of near-term volatility due to the $1 / T$ factor in the generalized formula used in the VIX1D Index calculation. As a result, when the time to expiration for the near-term (current day expiry) is less than 60 business minutes (at approximately 3:00 p.m. ET), the single-term volatility of the near term will be the last valid value and persisted until the near-term expiration time. During this period, the VIX1D Index will be the interpolation between the persisted near-term volatility and the next-term volatility, where the weights are heavily concentrated on the next-term. At the near-term expiration time, the VIX1D Index will fully converge to the volatility of the next term.

## Calculation of the VIX1D Index After Near-Term Expired

After the near-term contracts expired, at approximately 4:00 p.m. ET, the near-term leg (current day expiry) will no longer exist and the VIX1D Index will be calculated from 4:00 p.m. ET to 4:15 p.m. ET using only a single expiration - the next-term expiry. The formerly persisted near-term volatility will not be used in the calculation after 4:00 p.m ET.

## Use of Business Year and Minutes vs. Calendar Year and Minutes

The calculation of the VIX1D Index uses business years and business minutes during the Regular Trading Hours (RTH) session. As a result, the time component for the VIX1D Index is measured in a different increment than the VIX Index, which uses calendar years and calendar minutes.

## The Volatility of the VIX1D Index

By its nature, the VIX1D Index is expected to generally behave in a more volatile manner than indexes that measure a longer period of expected volatility. One reason for this is that the news events that affect the S\&P 500 Index on a given day are expected to have a larger impact on the short-dated SPX options than on longer dated options when market participants have more time to react to the news event.

## Supporting Documents

This Methodology references and should be read in conjunction with the following document:

## Cboe Volatility Index Mathematics Methodology

## The VIX1D Index Attributes

In this section, some of the configurations used for the Cboe 1-Day Volatility Index ${ }^{\circledR}$ (VIX1D Index) are provided.

## Contracts Used for the Near and Next Terms and Their Selection Method

The table below provides the attributes used for the near and next term selection for the VIX1D Index.

| Index | Constant Maturity | Set of Contracts Used for Constituent Series Selection | Selection Method |
| :--- | :--- | :--- | :--- |
| VIX1D | 1 day | PM-settled SPXW option contracts | Nearest Term Method |

## Table Key

- Constant Maturity: reflects the target expected volatility term
- Set of Contracts Used for Constituent Series Selection: provides the initial set of series that are candidates for the near and next term selection


## Market Data

The table below provides the source of the market data for all options series used in the VIX1D Index calculation. The market data used can be sourced from a specific exchange, from a subset of exchanges or from among all available exchanges or trading venues reflecting the (National) Best Bid/Offer ((N)BBO) quotes.

| Index | Market data source |
| :--- | :--- |
| VIX1D | Cboe Options Exchange (C1) data <br> via OPRA |

## Calculation and Dissemination

The calculation and dissemination of volatility index values is determined by trading session, e.g., regular trading hours (RTH), global trading hours (GTH) or both. The trading session(s) and approximate dissemination and calculation time periods are listed below. These times may be modified due to shortened trading sessions, e.g., shortened holiday trading hours. Calculation and dissemination occur approximately four times per minute. A Business Day is defined as a day when the Cboe Options Exchange is open for the Cboe Regular Trading Hours (RTH) session. The Index follows the Cboe Options Exchange holiday schedule.

| Index | Trading Session(s) | Approximate Calculation and Dissemination Time Period |
| :--- | :--- | :--- |
| VIX1D | RTH | Between 9:31 a.m. and 4:15 p.m. ET |

## The VIX1D Index Calculation: Step-by-Step

Stock indexes, such as the S\&P 500 Index, are calculated using the prices of their component stocks. Each index employs rulesthat govern the selection of component securities and a formula to calculate index values.

The VIX1D Index is a volatility index comprised of options rather than stocks, with the price of each option reflecting the market's expectation of future volatility. Like conventional indexes, the VIX1D Index calculation employs rules for selecting component options and a formula to calculate index values.

The generalized formula used in the VIX1D Index calculation ${ }^{\S}$ is:

$$
\sigma^{2}=\frac{2}{T} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{R T} Q\left(K_{i}\right)-\frac{1}{T}\left[\frac{F}{K_{0}}-1\right]^{2}
$$

where

$\sigma \quad$ VIX1D index $\sigma=\sigma \times 100 \quad \Delta K_{i} \quad$| Interval between strike prices - half the |
| :--- |
| difference between the strike on either side of $K_{i}:$ |

$T$ Time to expiration (in business years)
$F \quad$ Option-implied forward price
$K_{0}$ First strike equal to or otherwise immediately below the forward index level, F
$K_{i}$ Strike price of the $i^{\text {th }}$ out-of-the-money option; a call if $\mathrm{K}_{\mathrm{i}}>\mathrm{K}_{0}$ and a put if $\mathrm{K}_{\mathrm{i}}<\mathrm{K}_{0}$; both put and call if $\mathrm{Ki}=\mathrm{Ko}$.

[^0]The VIX1D Index measures 1-day expected volatility of the S\&P 500 Index. The calculation takes as input the market prices of SPXW options and U.S. Treasury yield curve rates. The VIX1D Index value can be obtained by following the four steps below:

## Step 1. Select the Near- and Next-Term

The universe of options that can be selected as components of the VIX1D Index are all PM-settled SPXW option contracts. The "near-term" options are defined to be the options where expiry date is equal to current day of calculation. The "next-term" options are defined to be the options within the remaining set expiring closest to and after the "near-term" options expiration date. Details can be found in section 1(b) Nearest Term Method of the Cboe Volatility Index Mathematics Methodology document. Contracts originally set to expire on unplanned closures will not be selected as near- or next-term contracts.

## Step 2. Calculate the Interest Rates

The risk-free interest rates, R1 and R2, are based on U.S. Treasury yield curve rates (commonly referred to as "Constant Maturity Treasury" rates, or CMTs), to which a cubic spline is applied to derive yields on the expiration dates of relevant SPXW options. As such, the VIX1D Index calculation may use different risk-free interest rates for near- and next-term options. The rules for calculating the interest rates for the near- and next-terms can be found in section 2(a) Interest Rate Calculation - Bounded Cubic Spline Interpolation of the Cboe Volatility Index Mathematics Methodology.

## Step 3. Calculate the Near- and Next-Term Variances

The inputs for calculating the variances for both terms $\sigma_{1}^{2}$ and $\sigma_{2}^{2}$ are based on the options series defined in Step 1 above. These include the corresponding bid, ask, and options price for each options series, where options price is defined as the midpoint of the bid / ask quotes, and the corresponding interest rates defined in Step 2 above. Given these inputs, the variances for the near- and next-terms can be calculated by following the steps outlined in section 3(a) Volatility Index Calculation - Single Term of the Cboe Volatility Index Mathematics Methodology.

Unlike other volatility indexes, the VIX1D Index calculation measures time to expiration of a constituent option series, $T$, in business years and business minutes (vs. calendar years and calendar minutes). This step is described in Step 3(a)(i) Time to Expiration of the Cboe Volatility Index Mathematics Methodology and is applied as set forth below in business years / business minutes. The time to expiration, $T$, is given by the following:

$$
T=\left(M_{\text {Time to Expiry }}\right) / M_{\text {year }}
$$

where

> | $M_{\text {Time to Expiry }}$ | Number of business minutes during RTH session from time of calculation until expiration |
| :---: | :---: |
| $M_{y e a r}$ | Number of business minutes during RTH session in a year $(252 \times 6.75 \times 60=102,060)$ |

The value of $\sigma_{1}^{2}$ is calculated based on the method described above when $M_{\text {Time to Expiry }} \geq 60$. If $M_{\text {Time to Expiry }}<60$, $\sigma_{1}^{2}$ will be the last valid $\sigma_{1}^{2}$ calculated when $M_{\text {Time to Expiry }} \geq 60$.

## Step 4. Calculate the VIX1D Index

- The inputs for calculating the VIX1D Index are based on the near- and next-term expiration dates defined in Step 1 above and the variances for each term calculated in Step 3 above. Given these inputs, the VIX1D Index is calculated as follows:

$$
\text { VIX1D }=100 \times \sqrt{\left\{T_{1} \sigma_{1}^{2}\left[\frac{M_{T_{2}}-M_{\mathrm{CM}}}{M_{T_{2}}-M_{T_{1}}}\right]+T_{2} \sigma_{2}^{2}\left[\frac{M_{\mathrm{CM}}-M_{T_{1}}}{M_{T_{2}}-M_{T_{1}}}\right]\right\} \times \frac{M_{\text {year }}}{M_{\mathrm{CM}}}}
$$

where

| $M_{T_{1}}$ | The number of business minutes until expiration of the near-term options |
| :--- | :--- |
| $M_{T_{2}}$ | The number of business minutes until expiration of the next-term options |
| $M_{\mathrm{CM}}$ | The number of business minutes during RTH session $(6.75 \times 60=405)$ |
| $M_{\text {year }}$ | The number of business minutes in one year $(252 \times 6.75 \times 60=102,060)$ |
| $T_{i}$ | $M_{T_{i}} / M_{y \text { ear }}$ |
| $\sigma_{i}^{2}$ | Variance of the $\mathrm{i}^{\text {th }}$ term calculated on Step 3 |

In order to avoid extrapolations in this calculation, when $M_{T_{2}}<M_{\mathrm{CM}}$, VIX1D should be calculated based on the next term only: VIX1D $=100 \times \sqrt{\sigma_{2}^{2}}$.

## Sample Calculation for the VIX1D Index

In this section, we implement a sample calculation for the VIX1D Index using the process outlined above.

- Select the Near- and Next-Term Constituent Series

In this hypothetical example, assume that the calculation is performed on trade date of September 27, 2022 at 11:00:00 a.m. ET. Given the inputs described in the Step 1 above, and the methodology in section 1(b) of the Cboe Volatility Index Mathematics Methodology, the selected terms for this calculation are the SPXW options expiring on Tuesday, September 27, 2022 for the near term and the SPXW options expiring on the following day (Wednesday, September 28, 2022) for the next term.

- Calculate the Interest Rates

Assume that the yield curve rates provided below are available on Monday, September 26, 2022 at the end of the day.

| Date | $\mathbf{1} \mathbf{~ M o}$ | $\mathbf{2 ~ M o}$ | $\mathbf{3} \mathbf{~ M o}$ | $\mathbf{6} \mathbf{~ M o}$ | $\mathbf{1} \mathbf{~ Y r}$ | $\mathbf{2} \mathbf{~ Y r}$ | $\mathbf{3} \mathbf{~ Y r}$ | $\mathbf{5} \mathbf{~ Y r}$ | $\mathbf{7} \mathbf{~ Y r}$ | $\mathbf{1 0} \mathbf{~ Y r}$ | $\mathbf{2 0} \mathbf{~ Y r}$ | $\mathbf{3 0} \mathbf{~ Y r}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $9 / 26 / 2022$ | 0.03 | 0.02 | 0.04 | 0.05 | 0.08 | 0.11 | 0.22 | 0.59 | 1 | 1.37 | 2.03 | 2.21 |

Given these yield curve rates, and the rules outlined in the section 2(a) of the Cboe Volatility Index Mathematics Methodology, the results are $\mathrm{R}_{1}=0.0393 \%$ for the near-term options and $\mathrm{R}_{2}=0.0390 \%$ for the next-term options.

## - Calculate the Single Term Variances

Time to Expiration
Following the steps described on Step 3 of the section "The VIX1D Index Calculation: Step-by-Step" for calculating time to expiration in business minutes and applying 11:00:00 a.m. ET as the time of the calculation, the time to expiration for the near-term and next-term options, $T_{1}$ and $T_{2}$, respectively, are:

$$
\begin{aligned}
& T_{1}=300 / 102,060=0.00293945 \\
& T_{2}=705 / 102,060=0.00690770
\end{aligned}
$$

Forward Price and $\mathrm{K}_{0}$
Using the call and put prices for the near-term and next-term options below and following the steps in Forward Price and $\mathrm{K}_{0}$ in section 3(a)(ii) Volatility Index Calculation - Single Term of the Cboe Volatility Index Mathematics Methodology, we can calculate the forward price and $\mathrm{K}_{0}$.

| Near Term Options |  |  |  |
| :---: | :---: | :---: | :---: |
| Strike Price | Call | Put | Difference |
| 3980 | 25.7 | 2.73 | 22.975 |
| 3985 | 21.65 | 3.60 | 18.05 |
| 3990 | 17.75 | 4.70 | 13.05 |
| 3995 | 14.2 | 6.15 | 8.05 |
| 4000 | 11 | 8.00 | 3 |
| 4005 | 8.3 | 10.3 | -2 |
| 4010 | 6.1 | 13.00 | -6.9 |
| 4015 | 4.25 | 16.30 | -12.05 |
| 4020 | 2.8 | 19.80 | -17 |


| Next Term Options |  |  |  |
| :---: | :---: | :---: | :---: |
| Strike Price | Call | Put | Difference |
| 3980 | 33.2 | 9.1 | 24.1 |
| 3985 | 29.7 | 10.6 | 19.05 |
| 3990 | 26.3 | 12.3 | 14.05 |
| 3995 | 23.2 | 14.1 | 9.1 |
| 4000 | 20.2 | 16.0 | 4.15 |
| 4005 | 17.3 | 18.25 | -0.95 |
| 4010 | 14.8 | 20.7 | -5.9 |
| 4015 | 12.4 | 23.3 | -10.9 |
| 4020 | 10.2 | 26.2 | -15.95 |

The ATM strike for the near-term options is 4005 and the ATM strike for the next-term options is 4005 . Applying their respective call and put prices to the formula

$$
F=\text { Strike Price }+e^{R T} \times(\text { Call Price }- \text { Put Price })
$$

gives that the forward index prices, $F_{1}$ and $F_{2}$, for the near- and next-term options, respectively, are:

$$
\begin{gathered}
F_{1}=4005+e^{(0.000393 \times 0.00293945)} \times(8.3-10.3)=4002.999998 \\
F_{2}=4005+e^{(0.000390 \times 0.00690770)} \times(17.3-18.25)=4004.049997
\end{gathered}
$$

We have then that $K_{0}$, the strike price equal to or immediately below the forward index level $F$, is 4000 for the near-term options and $\mathbf{4 0 0 0}$ for the next-term options.

## Strike Selection

To determine the strikes to be included in this calculation, refer to the steps in Strike Selection of section 3(a)(iii) Volatility Index Calculation - Single Term in the Cboe Volatility Index Mathematics Methodology.

First, for each term, select out-of-the-money put options with strike prices less than $K_{0}$. Start with the put strike immediately lower than $K_{0}$ and move to successively lower strike prices. Exclude any put option that has a bid price equal to zero (i.e., no bid). As shown below, once two puts with consecutive strike prices are found to have zero bid prices, exclude the observed put(s) and consider no puts with lower strikes for inclusion.

| Put Strike |  | Aid | Include? |
| :---: | :---: | :---: | :---: |
| 3845 | 0.00 | 0.05 |  |
| 3850 | 0.00 | 0.05 | Not considered following two zero bids |
| 3855 | 0.00 | 0.05 |  |
| 3860 | 0.00 | 0.05 | No |
| 3865 | 0.00 | 0.05 | No |
| 3870 | 0.05 | 0.10 | Yes |
| 3875 | 0.05 | 0.10 | Yes |
| 3880 | 0.00 | 0.10 | No |
| 3885 | 0.05 | 0.10 | Yes |

Next, select out-of-the-money call options with strike prices greater than $K_{0}$. Start with the call strike immediately higher than $K_{0}$ and move to successively higher strike prices, excluding call options that have a bid price of zero (i.e., no bid). As with the puts, once two call options with consecutive strike prices are found to have zero bid prices, exclude the observed call(s) and consider no calls with higher strikes for inclusion.

| Call Strike |  | Aid | Include? |
| :---: | :---: | :---: | :---: |
| 4060 | 0.05 | 0.10 | Yes |
| 4065 | 0.05 | 0.10 | Yes |
| 4070 | 0.00 | 0.10 | No |
| 4075 | 0.05 | 0.10 | Yes |
| 4080 | 0.00 | 0.05 | No |
| 4085 | 0.00 | 0.05 | No |
| 4090 | 0.00 | 0.05 | Not considered following two zero bids |
| 4095 | 0.00 | 0.05 |  |

Finally, select both the put and call with strike price $K_{0}$. Notice that two options are selected at $K_{0}$, while a single option, either a put or a call, is used for every other strike price.

The following tables contain the options used to calculate the VIX1D Index in this example. This calculation uses the midpoint of quoted bid and ask prices for each option selected. The $K_{0}$ put and call prices are averaged to produce a single value. The price used for the 4000 strike in the near-term is, therefore, $(11.00+8.00) / 2=9.5$. The price used for the 4000 strike in the next term is $(20.15+16.0) / 2=18.075$.

| Near-Term Strike | Option Type | Midpoint Price | Next-Term Strike | Option Type | Midpoint Price |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3870 | Put | 0.075 | 3650 | Put | 0.075 |
| 3875 | Put | 0.075 | 3660 | Put | 0.075 |
| 3885 | Put | 0.075 | 3670 | Put | 0.075 |
| . | . | - | - | - | - |
| 3990 | Put | 4.7 | 3990 | Put | 12.25 |
| 3995 | Put | 6.15 | 3995 | Put | 14.05 |
| 4000 | Put/Call Average | 9.5 | 4000 | Put/Call Average | 18.075 |
| 4005 | Call | 8.3 | 4005 | Call | 17.3 |


| 4010 | Call | 6.1 | 4010 | Call | 14.75 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| - | - | . | $\cdot$ |  | . |
| 4060 | Call | 0.075 | 4120 | Call | 0.1 |
| 4065 | Call | 0.075 | 4125 | Call | 0.075 |
| 4075 | Call | 0.075 | 4130 | Call | 0.075 |

## Calculating Volatility

The VIX1D Index is an amalgam of the information reflected in the prices of all of the selected options. The contribution of a single option to the VIX1D Index value is proportional to $\Delta K$ and the price of that option, and inversely proportional to the square of the option's strike price.

Referring to Calculating Volatility of section 3(a)(iv) Volatility Index Calculation - Single Term of the Cboe Volatility Index Mathematics Methodology, we generally have that $\Delta K_{i}$ is half the difference between the strike prices on either side of $K_{i}$. For example, the $\Delta K$ for the near-term 3875 Put is 7.5: $\Delta K_{3875 \text { Put }}=(3885-$ 3870) / 2. At the upper and lower edges of any given strip of options, $\Delta K_{i}$ is simply the difference between $K_{i}$ and the adjacent strike price. In this example, the 3870 Put is the lowest strike in the strip of near-term options and 3875 is the adjacent strike. Therefore, $\Delta K_{3870 \text { Put }}=5$ (i.e., $1375-1370$ ).

The contribution of the near-term 1370 Put is given by: $\frac{\Delta K_{3870 \text { Put }}^{K_{3870}^{2} \text { Put }} e^{R_{1} T_{1}} Q(3870 \text { Put }) ~}{\text { P }}$

$$
\frac{\Delta K_{3870 \text { Put }}}{K_{3870 \text { Put }}^{2}} e^{R_{1} T_{1}} Q(3870 \text { Put })=\frac{5}{(3870)^{2}} e^{(0.000393 x 0.00293945)}(0.075)=0.000000025
$$

A similar calculation is performed for each option. The resulting values for the near-term options are then summed and multiplied by $2 / \mathrm{T} 1$. Likewise, the resulting values for the next-term options are summed and multiplied by $2 / \mathrm{T} 2$. The tables below summarize the results for each set of options.

| Near-Term <br> Strike | Option Type | Midpoint <br> Price | Contribution <br> by Strike |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3870 | Put | 0.075 | 0.000000025 |  |  |  |
| 3875 | Put | 0.075 | 0.000000037 |  |  |  |
| 3885 | Put | 0.075 | 0.000000037 |  |  |  |
| $\cdot$ | $\cdot$ | $\cdot$ | $\cdot$ |  |  |  |
| 3990 | Put | 4.7 | 0.000001476 |  |  |  |
| 3995 | Put | 6.15 | 0.000001927 |  |  |  |
| 4000 | Put/Call Average | 9.500 | 0.000002969 |  |  |  |
| 4005 | Call | 8.3 | 0.000002587 |  |  |  |
| 4010 | Call | 6.1 | 0.000001897 |  |  |  |
| $\cdot$ | $\cdot$ | $\cdot$ | $\cdot$ |  |  |  |
| 4060 | Call | 0.075 | 0.000000023 |  |  |  |
| 4065 | Call | 0.075 | 0.000000034 |  |  |  |
| 4075 | Call | 0.075 | 0.000000045 |  |  |  |
| $\frac{\Delta K_{i}}{T_{1}} \sum_{i} \frac{R_{1} T_{1}}{K_{i}^{2}} Q\left(K_{i}\right)$ |  |  |  |  |  | 0.013281 |


| Next-Term Strike | Option Type | Midpoint Price | Contribution by Strike |
| :---: | :---: | :---: | :---: |
| 3650 | Put | 0.075 | 0.000000056 |
| 3660 | Put | 0.075 | 0.000000056 |
| 3670 | Put | 0.075 | 0.000000042 |
| - | . | - | - |
| 3990 | Put | 12.25 | 0.000003847 |
| 3995 | Put | 14.05 | 0.000004402 |
| 4000 | Put/Call Average | 18.075 | 0.000005648 |
| 4005 | Call | 17.3 | 0.000005393 |
| 4010 | Call | 14.75 | 0.000004586 |
| - | - | . |  |
| 4120 | Call | 0.1 | 0.000000044 |
| 4125 | Call | 0.075 | 0.000000022 |
| 4130 | Call | 0.075 | 0.000000022 |
| $\frac{2}{T_{2}} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{R_{2} T_{2}} Q\left(K_{i}\right)$ |  |  | 0.019303 |

Next calculate $1 / T\left[F / K_{0}-1\right]^{2}$ for the near-term ( $\mathrm{T}_{1}$ ) and next-term ( $\mathrm{T}_{2}$ ):

$$
\frac{1}{T_{1}}\left[\frac{F_{1}}{K_{0,1}}-1\right]^{2}=\frac{1}{0.00293945}\left[\frac{4002.999998}{4000}-1\right]^{2}=0.00019136
$$

$$
\frac{1}{T_{2}}\left[\frac{F_{2}}{K_{0,2}}-1\right]^{2}=\frac{1}{0.0069077}\left[\frac{4004.049997}{4000}-1\right]^{2}=0.00014841
$$

Now calculate $\sigma^{2} 1$ and $\sigma^{2}$ :

$$
\begin{aligned}
& \sigma_{1}^{2}=\frac{2}{T_{1}} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{R_{1} T_{1}} Q\left(K_{i}\right)-\frac{1}{T_{1}}\left[\frac{F_{1}}{K_{0,1}}-1\right]^{2}=0.01328108-0.00019136=0.01308972 \\
& \sigma_{2}^{2}=\frac{2}{T_{2}} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{R_{2} T_{2}} Q\left(K_{i}\right)-\frac{1}{T_{2}}\left[\frac{F_{2}}{K_{0,2}}-1\right]^{2}=0.01930298-0.00014841=0.01915457
\end{aligned}
$$

## - Calculate the VIX1D Index

The VIX1D Index value is now calculated by following Step 4 of the section "The VIX1D Index Calculation: Step-byStep". First, calculate the 1-day weighted average of $\sigma_{1}^{2}$ and $\sigma_{2}^{2}$. Then take the square root of that value and multiply by 100 :
$V I X 1 D=100 \times \sqrt{\left\{0.00293945 \times 0.01308972 \times\left[\frac{705-405}{705-300}\right]+0.0069077 \times 0.01915457 \times\left[\frac{405-300}{705-300}\right]\right\} \times \frac{102,060}{405}}$

$$
\text { VIX1D }=100 \times 0.1258046=12.58
$$

## Volatility Index Filtering Algorithm

From time to time, options price quotations widen due to changing market conditions, technology failures, or other reasons. When this occurs, options that were previously included in a VIX1D Index value calculation might be excluded due to them now having a zero bid price. This can result in a VIX1D Index value that, while accurately reflecting SPXW options quotes at the time, may not reflect the one day expected volatility of the S\&P 500 Index. Cboe uses a filtering algorithm to address these circumstances.

For the rules that guide this filtering process, refer to the details given in section "Index Level Filtering Algorithm" of the Cboe Volatility Index Mathematics Methodology. At a minimum annually, we review the thresholds used in the Index Level Filtering Algorithm to consider their reflection of market conditions, and may, in our discretion, change these thresholds as a result, by notice to clients from time to time. The inputs itemized below apply to the VIX1D Index:

| Index | Session | Threshold Level $(x)$ | Threshold Period |
| :---: | :---: | :---: | :---: |
| VIX1D | RTH | 1.00 volatility points | 1 minute |

## Exception When VIX1D Index Cannot be Calculated

In the event the VIX1D Index cannot be calculated, the last calculated and disseminated spot VIX1D Index value is republished until a new valid spot VIX1D Index can be calculated. The conditions that would prevent the VIX1D Index from being calculated can be found in sections 3(a) (ii) and (iii) Volatility Index Calculation - Single Term of the Cboe Volatility Index Mathematics Methodology. A summary can also be found in the section 4(b) Volatility Index Cannot be Calculated of the Cboe Volatility Index Mathematics Methodology.

Appendix 1: Complete SPXW Option Data Used in Sample VIX1D Index Calculation
Option series included in the VIX1D Index calculation are

| Near-Term Options |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Strike | Calls |  | Puts |  |
|  | Bid | Ask | Bid | Ask |
| 3625 | 377.4 | 378.5 | 0 | 0.05 |
| 3630 | 372.4 | 373.5 | 0 | 0.05 |
| 3640 | 362.4 | 363.5 | 0 | 0.05 |
| 3650 | 352.4 | 353.5 | 0 | 0.05 |
| 3660 | 342.4 | 343.5 | 0 | 0.05 |
| 3670 | 332.4 | 333.5 | 0 | 0.05 |
| 3675 | 327.4 | 328.5 | 0 | 0.05 |
| 3680 | 322.4 | 323.5 | 0 | 0.05 |
| 3690 | 312.4 | 313.5 | 0 | 0.05 |
| 3695 | 307.4 | 308.5 | 0 | 0.05 |
| 3700 | 302.4 | 303.5 | 0 | 0.05 |
| 3705 | 297.4 | 298.5 | 0 | 0.05 |
| 3710 | 292.4 | 293.5 | 0 | 0.05 |
| 3715 | 287.4 | 288.5 | 0 | 0.05 |
| 3720 | 282.4 | 283.5 | 0 | 0.05 |
| 3725 | 277.4 | 278.5 | 0 | 0.05 |
| 3730 | 272.4 | 273.5 | 0 | 0.05 |
| 3735 | 267.4 | 268.5 | 0 | 0.05 |
| 3740 | 262.4 | 263.5 | 0 | 0.05 |
| 3745 | 257.4 | 258.5 | 0 | 0.05 |
| 3750 | 252.4 | 253.5 | 0 | 0.05 |
| 3755 | 247.4 | 248.5 | 0 | 0.05 |
| 3760 | 242.4 | 243.5 | 0 | 0.05 |
| 3765 | 237.4 | 238.5 | 0 | 0.05 |
| 3770 | 232.4 | 233.5 | 0 | 0.05 |
| 3775 | 227.4 | 228.5 | 0 | 0.05 |
| 3780 | 222.4 | 223.5 | 0 | 0.05 |
| 3785 | 217.4 | 218.5 | 0 | 0.05 |
| 3790 | 212.4 | 213.5 | 0 | 0.05 |
| 3795 | 207.4 | 208.5 | 0 | 0.05 |
| 3800 | 202.4 | 203.5 | 0 | 0.05 |
| 3805 | 197.4 | 198.5 | 0 | 0.05 |
| 3810 | 192.4 | 193.5 | 0 | 0.05 |
| 3815 | 187.4 | 188.5 | 0 | 0.05 |
| 3820 | 182.4 | 183.5 | 0 | 0.05 |
| 3825 | 177.4 | 178.5 | 0 | 0.05 |
| 3830 | 172.4 | 173.5 | 0 | 0.05 |
| 3835 | 167.4 | 168.5 | 0 | 0.05 |


| Next-Term Options |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Strike | Calls |  | Puts |  |
|  | Bid | Ask | Bid | Ask |
| 3550 | 453.4 | 454.5 | 0 | 0.05 |
| 3575 | 428.4 | 429.5 | 0.05 | 0.1 |
| 3600 | 403.4 | 404.5 | 0.05 | 0.1 |
| 3620 | 383.4 | 384.6 | 0.05 | 0.1 |
| 3625 | 378.4 | 379.6 | 0.05 | 0.1 |
| 3630 | 373.4 | 374.6 | 0 | 0.1 |
| 3640 | 363.4 | 364.6 | 0 | 0.1 |
| 3650 | 353.4 | 354.6 | 0.05 | 0.1 |
| 3660 | 343.4 | 344.6 | 0.05 | 0.1 |
| 3670 | 333.4 | 334.6 | 0.05 | 0.1 |
| 3675 | 328.4 | 329.6 | 0.05 | 0.1 |
| 3680 | 323.4 | 324.6 | 0.05 | 0.1 |
| 3690 | 313.4 | 314.6 | 0.05 | 0.1 |
| 3695 | 308.4 | 309.6 | 0.05 | 0.1 |
| 3700 | 303.4 | 304.6 | 0.05 | 0.1 |
| 3705 | 298.4 | 299.6 | 0.05 | 0.1 |
| 3710 | 293.5 | 294.6 | 0.05 | 0.1 |
| 3715 | 288.5 | 289.6 | 0.05 | 0.1 |
| 3720 | 283.5 | 284.6 | 0.05 | 0.1 |
| 3725 | 278.5 | 279.6 | 0.05 | 0.1 |
| 3730 | 273.5 | 274.6 | 0.05 | 0.15 |
| 3735 | 268.5 | 269.6 | 0.05 | 0.15 |
| 3740 | 263.5 | 264.6 | 0.1 | 0.15 |
| 3745 | 258.5 | 259.6 | 0.05 | 0.15 |
| 3750 | 253.5 | 254.6 | 0.05 | 0.15 |
| 3755 | 248.5 | 249.6 | 0.05 | 0.15 |
| 3760 | 243.5 | 244.6 | 0.05 | 0.15 |
| 3765 | 238.5 | 239.6 | 0.1 | 0.15 |
| 3770 | 233.5 | 234.6 | 0.1 | 0.15 |
| 3775 | 228.5 | 229.6 | 0.1 | 0.15 |
| 3780 | 223.5 | 224.7 | 0.1 | 0.15 |
| 3785 | 218.5 | 219.7 | 0.1 | 0.15 |
| 3790 | 213.5 | 214.7 | 0.1 | 0.15 |
| 3795 | 208.5 | 209.7 | 0.1 | 0.15 |
| 3800 | 203.5 | 204.7 | 0.1 | 0.2 |
| 3805 | 198.5 | 199.7 | 0.1 | 0.15 |
| 3810 | 193.5 | 194.7 | 0.1 | 0.2 |
| 3815 | 188.5 | 189.7 | 0.15 | 0.2 |


| Near-Term Options (cont.) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Strike | Calls |  | Puts |  |
|  | Bid | Ask | Bid | Ask |
| 3840 | 162.4 | 163.5 | 0 | 0.05 |
| 3845 | 157.4 | 158.5 | 0 | 0.05 |
| 3850 | 152.4 | 153.5 | 0 | 0.05 |
| 3855 | 147.4 | 148.6 | 0 | 0.05 |
| 3860 | 142.4 | 143.6 | 0 | 0.05 |
| 3865 | 137.4 | 138.6 | 0 | 0.05 |
| 3870 | 132.4 | 133.6 | 0.05 | 0.1 |
| 3875 | 127.4 | 128.6 | 0.05 | 0.1 |
| 3880 | 122.4 | 123.6 | 0 | 0.1 |
| 3885 | 117.4 | 118.6 | 0.05 | 0.1 |
| 3890 | 112.4 | 113.6 | 0.05 | 0.1 |
| 3895 | 107.5 | 108.5 | 0.05 | 0.1 |
| 3900 | 102.5 | 103.5 | 0.05 | 0.1 |
| 3905 | 97.5 | 98.4 | 0.05 | 0.1 |
| 3910 | 92.5 | 93.5 | 0.1 | 0.15 |
| 3915 | 87.5 | 88.5 | 0.1 | 0.15 |
| 3920 | 82.5 | 83.6 | 0.1 | 0.2 |
| 3925 | 77.6 | 78.6 | 0.15 | 0.2 |
| 3930 | 72.6 | 73.6 | 0.2 | 0.25 |
| 3935 | 67.7 | 68.6 | 0.25 | 0.3 |
| 3940 | 62.8 | 63.8 | 0.3 | 0.4 |
| 3945 | 57.8 | 58.9 | 0.4 | 0.5 |
| 3950 | 53.1 | 53.9 | 0.5 | 0.6 |
| 3955 | 48.1 | 49 | 0.7 | 0.75 |
| 3960 | 43.5 | 44.3 | 0.9 | 0.95 |
| 3965 | 38.7 | 39.6 | 1.15 | 1.25 |
| 3970 | 34.2 | 34.9 | 1.55 | 1.65 |
| 3975 | 29.7 | 30.3 | 2.05 | 2.1 |
| 3980 | 25.3 | 26.1 | 2.7 | 2.75 |
| 3985 | 21.4 | 21.9 | 3.5 | 3.7 |
| 3990 | 17.5 | 18 | 4.6 | 4.8 |
| 3995 | 14.1 | 14.3 | 6.1 | 6.2 |
| 4000 | 10.9 | 11.1 | 7.9 | 8.1 |
| 4005 | 8.2 | 8.4 | 10.2 | 10.4 |
| 4010 | 6 | 6.2 | 12.9 | 13.1 |
| 4015 | 4.2 | 4.3 | 16.1 | 16.5 |
| 4020 | 2.75 | 2.85 | 19.5 | 20.1 |
| 4025 | 1.7 | 1.8 | 23.4 | 24.1 |
| 4030 | 1 | 1.1 | 27.7 | 28.4 |
| 4035 | 0.6 | 0.65 | 32.3 | 33.2 |
| 4040 | 0.35 | 0.4 | 36.9 | 37.8 |
| 4045 | 0.2 | 0.25 | 41.9 | 42.8 |


| Next-Term Options (cont.) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Strike | Calls |  | Puts |  |
|  | Bid | Ask | Bid | Ask |
| 3820 | 183.6 | 184.7 | 0.15 | 0.2 |
| 3825 | 178.6 | 179.7 | 0.15 | 0.2 |
| 3830 | 173.6 | 174.7 | 0.15 | 0.25 |
| 3835 | 168.6 | 169.7 | 0.15 | 0.25 |
| 3840 | 163.6 | 164.7 | 0.2 | 0.25 |
| 3845 | 158.6 | 159.8 | 0.2 | 0.25 |
| 3850 | 153.6 | 154.8 | 0.2 | 0.3 |
| 3855 | 148.7 | 149.8 | 0.25 | 0.3 |
| 3860 | 143.7 | 144.8 | 0.25 | 0.35 |
| 3865 | 138.7 | 139.8 | 0.3 | 0.35 |
| 3870 | 133.7 | 134.9 | 0.3 | 0.4 |
| 3875 | 128.8 | 129.9 | 0.35 | 0.4 |
| 3880 | 123.8 | 125 | 0.4 | 0.45 |
| 3885 | 118.9 | 120 | 0.45 | 0.5 |
| 3890 | 113.9 | 115.1 | 0.5 | 0.55 |
| 3895 | 109.1 | 110.1 | 0.55 | 0.65 |
| 3900 | 104.1 | 105.2 | 0.65 | 0.7 |
| 3905 | 99.3 | 100.2 | 0.75 | 0.8 |
| 3910 | 94.3 | 95.4 | 0.85 | 0.95 |
| 3915 | 89.5 | 90.5 | 1 | 1.1 |
| 3920 | 84.7 | 85.6 | 1.2 | 1.25 |
| 3925 | 79.9 | 80.8 | 1.4 | 1.45 |
| 3930 | 75.2 | 76.1 | 1.65 | 1.75 |
| 3935 | 70.5 | 71.5 | 1.95 | 2.05 |
| 3940 | 65.9 | 66.7 | 2.3 | 2.4 |
| 3945 | 61.3 | 62.2 | 2.8 | 2.85 |
| 3950 | 56.9 | 57.8 | 3.3 | 3.5 |
| 3955 | 52.6 | 53.4 | 3.9 | 4.1 |
| 3960 | 48.3 | 49.2 | 4.7 | 4.9 |
| 3965 | 44.2 | 45 | 5.6 | 5.7 |
| 3970 | 40.3 | 41 | 6.6 | 6.8 |
| 3975 | 36.4 | 37.2 | 7.7 | 7.9 |
| 3980 | 32.8 | 33.6 | 9 | 9.2 |
| 3985 | 29.4 | 29.9 | 10.5 | 10.7 |
| 3990 | 26.2 | 26.4 | 12.2 | 12.3 |
| 3995 | 23 | 23.3 | 14 | 14.1 |
| 4000 | 20 | 20.3 | 15.9 | 16.1 |
| 4005 | 17.2 | 17.4 | 18.1 | 18.4 |
| 4010 | 14.6 | 14.9 | 20.5 | 20.8 |
| 4015 | 12.3 | 12.5 | 23.2 | 23.4 |
| 4020 | 10.1 | 10.3 | 26 | 26.3 |
| 4025 | 8.2 | 8.4 | 29.1 | 29.4 |


| 4050 | 0.15 | 0.2 | 46.8 | 47.7 |
| :--- | :--- | :--- | :--- | :--- |



| Next-Term Options (cont.) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Strike | Calls |  | Puts |  |
|  | Bid | Ask | Bid | Ask |
| 4035 | 5.2 | 5.4 | 35.8 | 36.7 |
| 4040 | 4 | 4.2 | 39.6 | 40.6 |
| 4045 | 3 | 3.2 | 43.7 | 44.6 |
| 4050 | 2.3 | 2.4 | 47.9 | 48.8 |
| 4055 | 1.75 | 1.85 | 52.4 | 53.3 |
| 4060 | 1.35 | 1.4 | 56.9 | 57.9 |
| 4065 | 0.95 | 1.05 | 61.6 | 62.5 |
| 4070 | 0.75 | 0.8 | 66.3 | 67.3 |
| 4075 | 0.55 | 0.65 | 71.1 | 72.1 |
| 4080 | 0.45 | 0.5 | 76 | 77 |
| 4085 | 0.35 | 0.4 | 80.9 | 81.9 |
| 4090 | 0.25 | 0.35 | 85.8 | 86.8 |
| 4100 | 0.15 | 0.25 | 95.8 | 96.8 |
| 4110 | 0.1 | 0.15 | 105.7 | 106.7 |
| 4120 | 0.05 | 0.15 | 115.5 | 116.6 |
| 4125 | 0.05 | 0.1 | 120.5 | 121.6 |
| 4130 | 0.05 | 0.1 | 125.5 | 126.6 |
| 4150 | 0 | 0.1 | 145.4 | 146.6 |
| 4175 | 0 | 0.05 | 170.4 | 171.6 |
| 4200 | 0 | 0.05 | 195.4 | 196.6 |

## Appendix 2: Individual Contributions

| Near- <br> Term <br> Strike | Option Type | Midpoint Price | Delta-K | Contribution by Strike |
| :---: | :---: | :---: | :---: | :---: |
| 3870 | Put | 0.075 | 5 | 0.0000000250 |
| 3875 | Put | 0.075 | 7.5 | 0.0000000375 |
| 3885 | Put | 0.075 | 7.5 | 0.0000000373 |
| 3890 | Put | 0.075 | 5 | 0.0000000248 |
| 3895 | Put | 0.075 | 5 | 0.0000000247 |
| 3900 | Put | 0.075 | 5 | 0.0000000247 |
| 3905 | Put | 0.075 | 5 | 0.0000000246 |
| 3910 | Put | 0.125 | 5 | 0.0000000409 |
| 3915 | Put | 0.125 | 5 | 0.0000000408 |
| 3920 | Put | 0.15 | 5 | 0.0000000488 |
| 3925 | Put | 0.175 | 5 | 0.0000000568 |
| 3930 | Put | 0.225 | 5 | 0.0000000728 |
| 3935 | Put | 0.275 | 5 | 0.0000000888 |
| 3940 | Put | 0.35 | 5 | 0.0000001127 |
| 3945 | Put | 0.45 | 5 | 0.0000001446 |
| 3950 | Put | 0.55 | 5 | 0.0000001763 |
| 3955 | Put | 0.725 | 5 | 0.0000002317 |
| 3960 | Put | 0.925 | 5 | 0.0000002949 |
| 3965 | Put | 1.2 | 5 | 0.0000003817 |
| 3970 | Put | 1.6 | 5 | 0.0000005076 |
| 3975 | Put | 2.075 | 5 | 0.0000006566 |
| 3980 | Put | 2.725 | 5 | 0.0000008601 |
| 3985 | Put | 3.6 | 5 | 0.0000011335 |
| 3990 | Put | 4.7 | 5 | 0.0000014761 |
| 3995 | Put | 6.15 | 5 | 0.0000019267 |
| 4000 | Put/Call Average | 9.5 | 5 | 0.0000029688 |
| 4005 | Call | 8.3 | 5 | 0.0000025873 |
| 4010 | Call | 6.1 | 5 | 0.0000018968 |
| 4015 | Call | 4.25 | 5 | 0.0000013182 |
| 4020 | Call | 2.8 | 5 | 0.0000008663 |
| 4025 | Call | 1.75 | 5 | 0.0000005401 |
| 4030 | Call | 1.05 | 5 | 0.0000003233 |
| 4035 | Call | 0.625 | 5 | 0.0000001919 |
| 4040 | Call | 0.375 | 5 | 0.0000001149 |
| 4045 | Call | 0.225 | 5 | 0.0000000688 |
| 4050 | Call | 0.175 | 5 | 0.0000000533 |
| 4055 | Call | 0.125 | 5 | 0.0000000380 |
| 4060 | Call | 0.075 | 5 | 0.0000000227 |
| 4065 | Call | 0.075 | 7.5 | 0.0000000340 |
| 4075 | Call | 0.075 | 10 | 0.0000000452 |


| Next- <br> Term <br> Strike | Option Type | Midpoint Price | Delta-K | Contributio n by Strike |
| :---: | :---: | :---: | :---: | :---: |
| 3650 | Put | 0.075 | 10 | 0.0000000563 |
| 3660 | Put | 0.075 | 10 | 0.0000000560 |
| 3670 | Put | 0.075 | 7.5 | 0.0000000418 |
| 3675 | Put | 0.075 | 5 | 0.0000000278 |
| 3680 | Put | 0.075 | 7.5 | 0.0000000415 |
| 3690 | Put | 0.075 | 7.5 | 0.0000000413 |
| 3695 | Put | 0.075 | 5 | 0.0000000275 |
| 3700 | Put | 0.075 | 5 | 0.0000000274 |
| 3705 | Put | 0.075 | 5 | 0.0000000273 |
| 3710 | Put | 0.075 | 5 | 0.0000000272 |
| 3715 | Put | 0.075 | 5 | 0.0000000272 |
| 3720 | Put | 0.075 | 5 | 0.0000000271 |
| 3725 | Put | 0.075 | 5 | 0.0000000270 |
| 3730 | Put | 0.1 | 5 | 0.0000000359 |
| 3735 | Put | 0.1 | 5 | 0.0000000358 |
| 3740 | Put | 0.125 | 5 | 0.0000000447 |
| 3745 | Put | 0.1 | 5 | 0.0000000357 |
| 3750 | Put | 0.1 | 5 | 0.0000000356 |
| 3755 | Put | 0.1 | 5 | 0.0000000355 |
| 3760 | Put | 0.1 | 5 | 0.0000000354 |
| 3765 | Put | 0.125 | 5 | 0.0000000441 |
| 3770 | Put | 0.125 | 5 | 0.0000000440 |
| 3775 | Put | 0.125 | 5 | 0.0000000439 |
| 3780 | Put | 0.125 | 5 | 0.0000000437 |
| 3785 | Put | 0.125 | 5 | 0.0000000436 |
| 3790 | Put | 0.125 | 5 | 0.0000000435 |
| 3795 | Put | 0.125 | 5 | 0.0000000434 |
| 3800 | Put | 0.15 | 5 | 0.0000000519 |
| 3805 | Put | 0.125 | 5 | 0.0000000432 |
| 3810 | Put | 0.15 | 5 | 0.0000000517 |
| 3815 | Put | 0.175 | 5 | 0.0000000601 |
| 3820 | Put | 0.175 | 5 | 0.0000000600 |
| 3825 | Put | 0.175 | 5 | 0.0000000598 |
| 3830 | Put | 0.2 | 5 | 0.0000000682 |
| 3835 | Put | 0.2 | 5 | 0.0000000680 |
| 3840 | Put | 0.225 | 5 | 0.0000000763 |
| 3845 | Put | 0.225 | 5 | 0.0000000761 |
| 3850 | Put | 0.25 | 5 | 0.0000000843 |
| 3855 | Put | 0.275 | 5 | 0.0000000925 |
| 3860 | Put | 0.3 | 5 | 0.0000001007 |


| Individual Contributions (Cont.) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Next- <br> Term <br> Strike | Option Type | Midpoint Price | Delta-K | Contribution by Strike |
| 3865 | Put | 0.325 | 5 | 0.0000001088 |
| 3870 | Put | 0.35 | 5 | 0.0000001168 |
| 3875 | Put | 0.375 | 5 | 0.0000001249 |
| 3880 | Put | 0.425 | 5 | 0.0000001412 |
| 3885 | Put | 0.475 | 5 | 0.0000001574 |
| 3890 | Put | 0.525 | 5 | 0.0000001735 |
| 3895 | Put | 0.6 | 5 | 0.0000001977 |
| 3900 | Put | 0.675 | 5 | 0.0000002219 |
| 3905 | Put | 0.775 | 5 | 0.0000002541 |
| 3910 | Put | 0.9 | 5 | 0.0000002943 |
| 3915 | Put | 1.05 | 5 | 0.0000003425 |
| 3920 | Put | 1.225 | 5 | 0.0000003986 |
| 3925 | Put | 1.425 | 5 | 0.0000004625 |
| 3930 | Put | 1.7 | 5 | 0.0000005503 |
| 3935 | Put | 2 | 5 | 0.0000006458 |
| 3940 | Put | 2.35 | 5 | 0.0000007569 |
| 3945 | Put | 2.825 | 5 | 0.0000009076 |
| 3950 | Put | 3.4 | 5 | 0.0000010896 |
| 3955 | Put | 4 | 5 | 0.0000012786 |
| 3960 | Put | 4.8 | 5 | 0.0000015305 |
| 3965 | Put | 5.65 | 5 | 0.0000017969 |
| 3970 | Put | 6.7 | 5 | 0.0000021255 |
| 3975 | Put | 7.8 | 5 | 0.0000024683 |
| 3980 | Put | 9.1 | 5 | 0.0000028724 |
| 3985 | Put | 10.6 | 5 | 0.0000033375 |
| 3990 | Put | 12.25 | 5 | 0.0000038473 |
| 3995 | Put | 14.05 | 5 | 0.0000044016 |
| 4000 | Put/Call <br> Average | 18.075 | 5 | 0.0000056485 |
| 4005 | Call | 17.3 | 5 | 0.0000053928 |
| 4010 | Call | 14.75 | 5 | 0.0000045864 |
| 4015 | Call | 12.4 | 5 | 0.0000038461 |
| 4020 | Call | 10.2 | 5 | 0.0000031559 |
| 4025 | Call | 8.3 | 5 | 0.0000025616 |
| 4030 | Call | 6.7 | 5 | 0.0000020627 |
| 4035 | Call | 5.3 | 5 | 0.0000016276 |
| 4040 | Call | 4.1 | 5 | 0.0000012560 |
| 4045 | Call | 3.1 | 5 | 0.0000009473 |
| 4050 | Call | 2.35 | 5 | 0.0000007164 |
| 4055 | Call | 1.8 | 5 | 0.0000005473 |
| 4060 | Call | 1.375 | 5 | 0.0000004171 |
| 4065 | Call | 1 | 5 | 0.0000003026 |
| 4070 | Call | 0.775 | 5 | 0.0000002339 |


| Individual Contributions (Cont.) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Next- <br> Term <br> Strike | Option Type | Midpoint <br> Price | Delta-K | Contribution <br> by Strike |
| 4075 | Call | 0.6 | 5 | 0.0000001807 |
| 4080 | Call | 0.475 | 5 | 0.0000001427 |
| 4085 | Call | 0.375 | 5 | 0.0000001124 |
| 4090 | Call | 0.3 | 7.5 | 0.0000001345 |
| 4100 | Call | 0.2 | 10 | 0.0000001190 |
| 4110 | Call | 0.125 | 10 | 0.0000000740 |
| 4120 | Call | 0.1 | 7.5 | 0.0000000442 |
| 4125 | Call | 0.075 | 5 | 0.0000000220 |
| 4130 | Call | 0.075 | 5 | 0.0000000220 |

Sum of Individual Contributions for near term: 0.0000195195
$\frac{2}{T_{1}} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{R_{1} T_{1}} Q\left(K_{i}\right)=0.0132811$
Sum of Individual Contributions for next term: 0.0000666696
$\frac{2}{T_{2}} \sum_{i} \frac{\Delta K_{i}}{K_{i}^{2}} e^{R_{2} T_{2}} Q\left(K_{i}\right)=0.0193030$

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[^0]:    ${ }^{\text {§ Please see "More than you ever wanted to know about volatility swaps" by Kresimir Demeterfi, Emanuel Derman, Michael }}$ Kamal, and Joseph Zou, Goldman Sachs Quantitative Strategies Research Notes, March 1999.

